

# **Kesetimbangan Uap/Cair: Pendahuluan**

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# Kesetimbangan Fase

- Aplikasi
  - Distilasi, absorpsi, dan ekstraksi → membuat kontak antar fase-fase yg berbeda
- Sejauh mana perubahan dan kecepatan transfer massa antar fase, tergantung pada keberangkatan sistem dari kesetimbangannya.
- Perhitungan kuantitatif transfer massa; T dan P saat kesetimbangan; dan komposisi tiap fase → harus diketahui

# Sifat Kesetimbangan

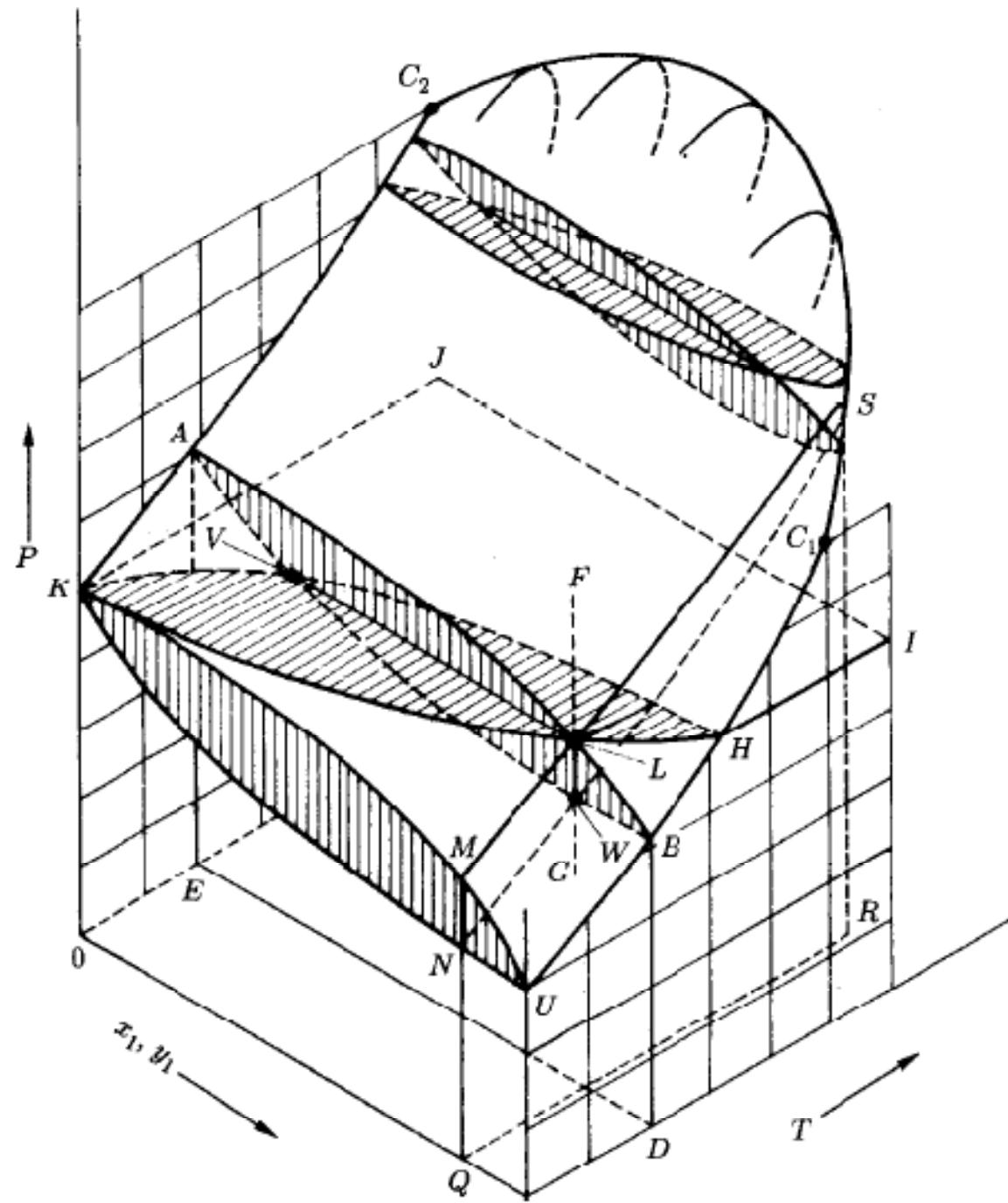
- Sebuah kondisi statis di mana tidak ada perubahan terjadi dalam sifat-sifat makroskopik sistem terhadap waktu.
- Pada tingkat mikroskopik, kondisi tidak statis.  
Transfer massa molekuler adalah sama pada kedua arah, dan secara netto transfer massa antarfase sama dgn nol.
- Sistem terisolasi yg terdiri dari fase cair & uap dalam kontak yg akhirnya mencapai keadaan di mana tdk ada kecenderungan perubahan terjadi di dlm sistem.  
Saat itu suhu, tekanan, dan komposisi fase tetap.

# Phase rule vs. Duhem's theorem

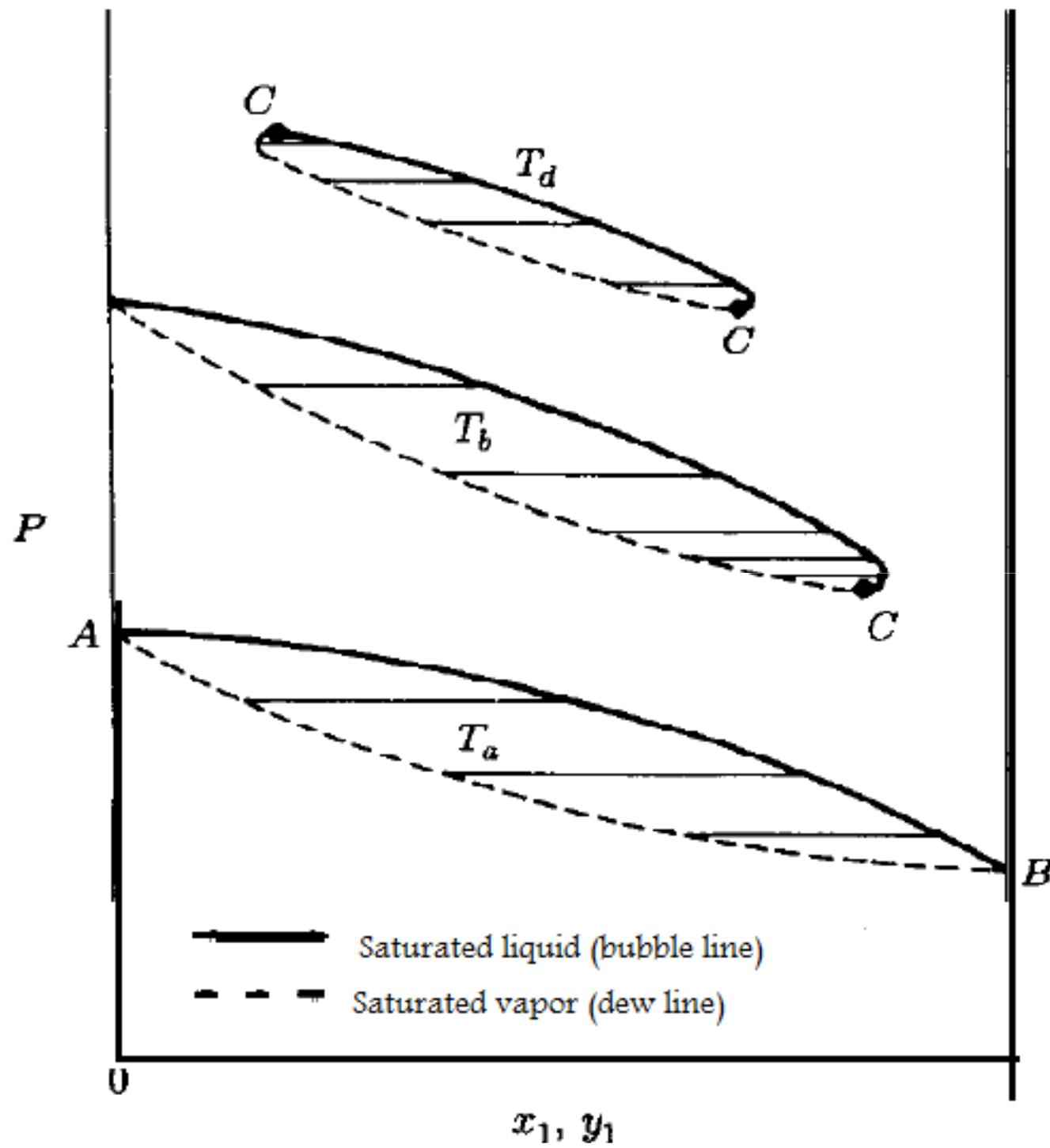
- (The number of variables that is independently fixed in a system at equilibrium) = (the number of variables that characterize the intensive state of the system) - (the number of independent equations connecting the variable):
- Phase rule: 
$$F = 2 + (N - 1)(\pi) - (\pi - 1)(N) = 2 - \pi + N$$
- Duhem's rule: 
$$F = 2 + [(N - 1)(\pi) + \pi] - [(\pi - 1)(N) + N] = 2$$
  - for any closed system formed initially from given masses of prescribed chemical species, the equilibrium state is completely determined when **any two** independent variables are fixed.
  - **Two ?** When phase rule  $F = 1$ , at least one of the two variables must be extensive, and when  $F = 0$ , both must be extensive.

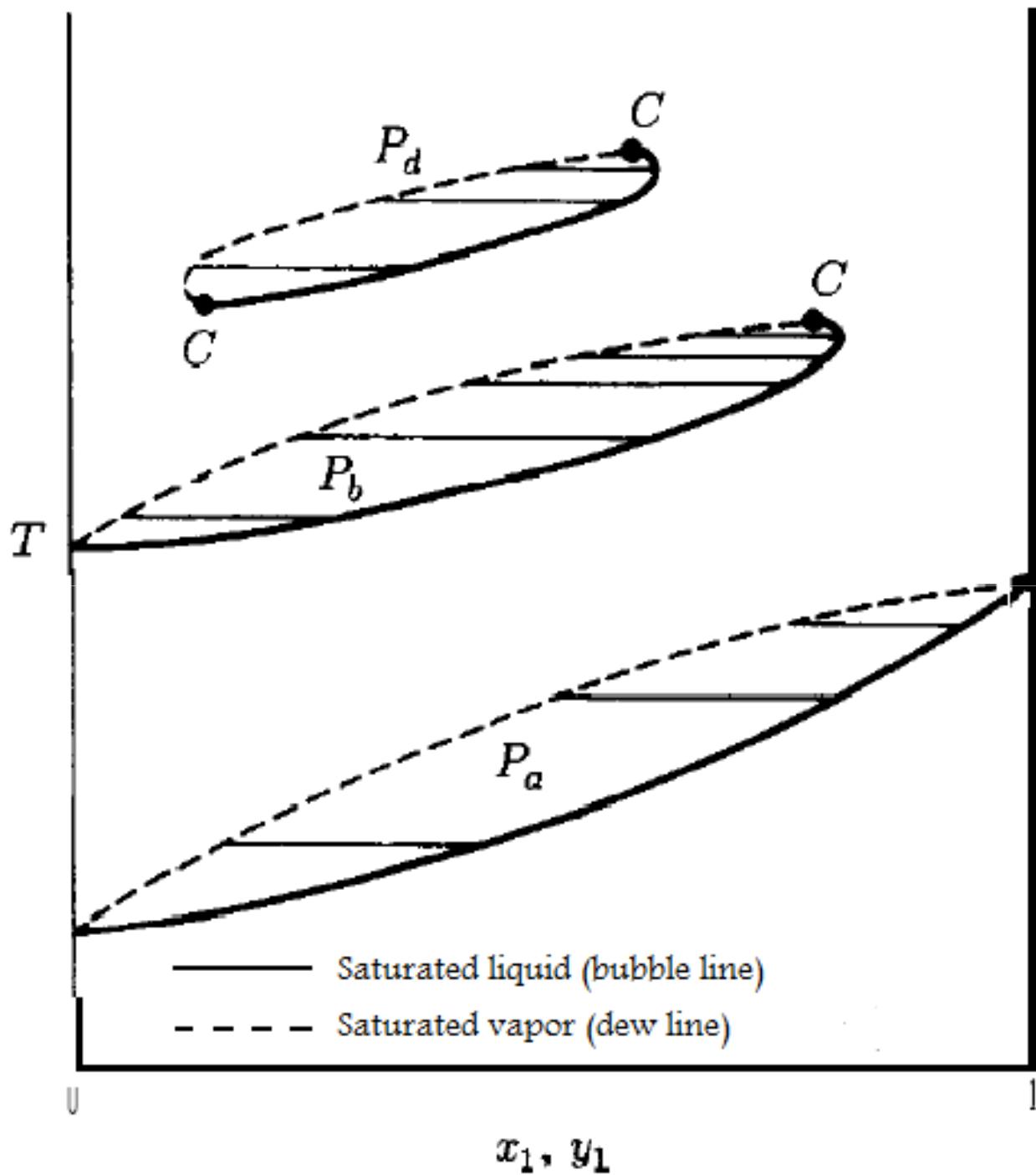
# VLE: qualitative behavior

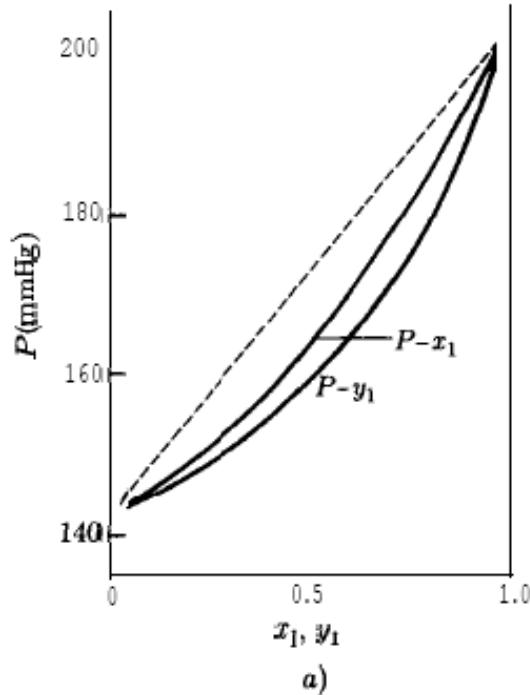
- When two chemical species:  $N = 2$ 
  - phase rule:  $F = 4 - \pi$
  - the maximum value of  $F = 3$  ( $\pi = 1$ ), namely, P, T, and one mole fraction. All equilibrium states of the system can be represented in three-dimensional P-T-composition space.



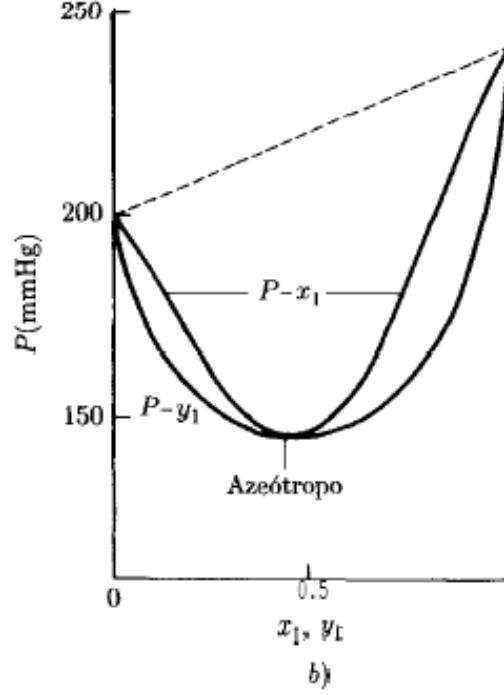
- Within this space, the states of pairs of phases coexisting at equilibrium define surfaces.
  - The subcooled-liquid region lies above the upper surface; the superheated-vapor region lies below the under surface.
  - $UBHC_1$  and  $KAC_2$  represent the vapor pressure-vs.-T curves for pure species 1 and 2.
  - $C_1$  and  $C_2$  are the critical points of pure species 1 and 2.
  - $L$  is a bubble point and the upper surface is the bubblepoint surface.
  - Line  $VL$  is an example of a tie line, which connects points representing phases in equilibrium.
  - $W$  is a dewpoint and the lower surface is the dewpoint surface.
- $Pxy$  diagram at constant T
- $Txy$  diagram at constant P
- $PT$  diagram at constant composition



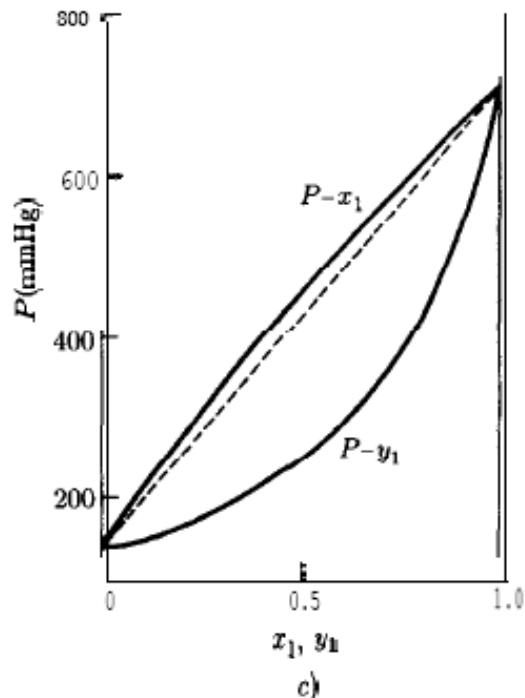




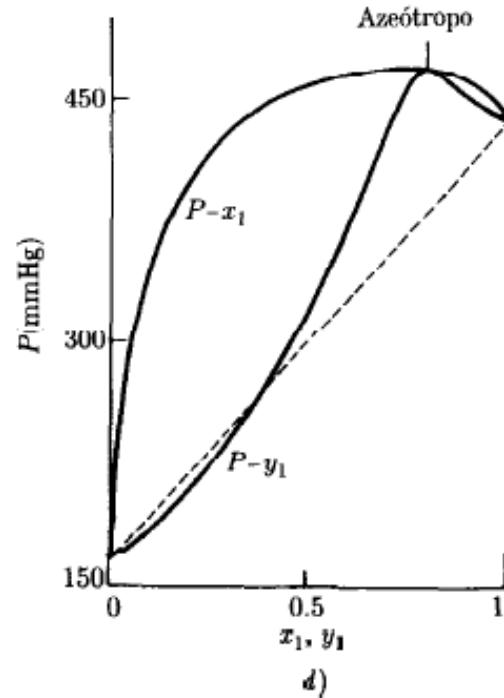
a)



b)

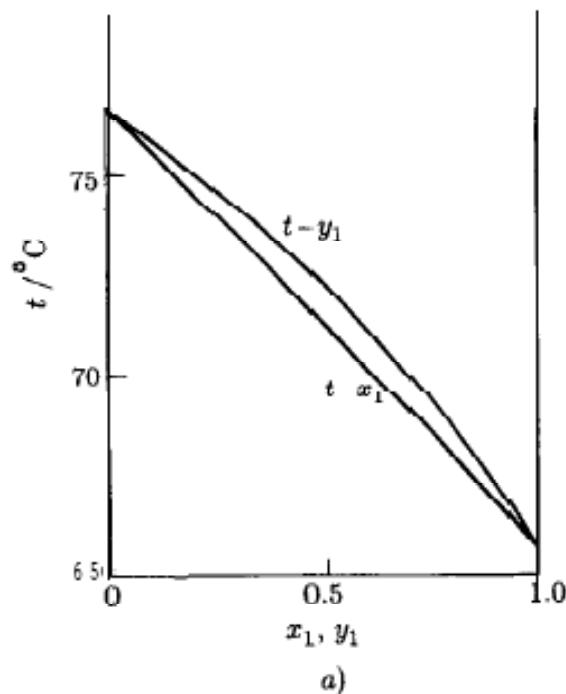


c)

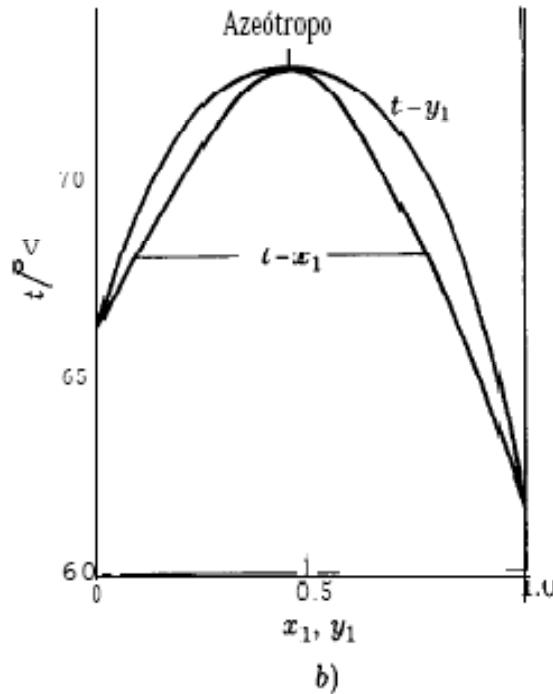


d)

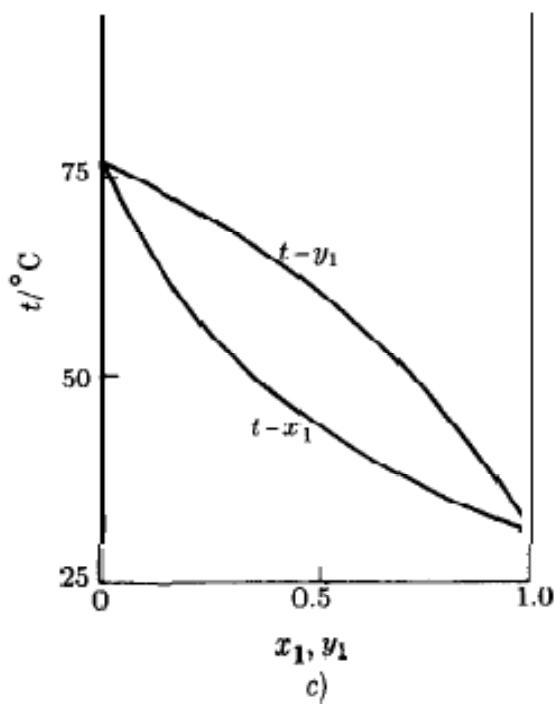
- Fig 10.8 (a)(b), Negative departures from  $P-x_1$  linearity: strong liquid-phase intermolecular attractions between unlike than between like pairs of molecules.
- Fig 10.8 (c)(d), Positive departures from  $P-x_1$  linearity: strong liquid-phase intermolecular attractions between like than between unlike pairs of molecules.
- Fig 10.8 (b)(d), the “azeotrope”: the point where  $x_1 = y_1$  the dewpoint and bubblepoint curves are tangent to the same horizontal line. The liquid does not change in composition as it evaporates. No separation of such a constant-boiling solution is possible by distillation.



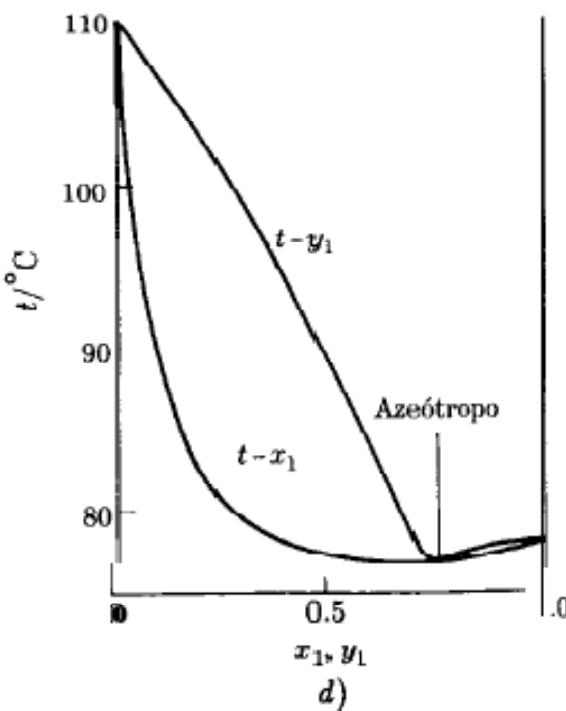
a)



b)

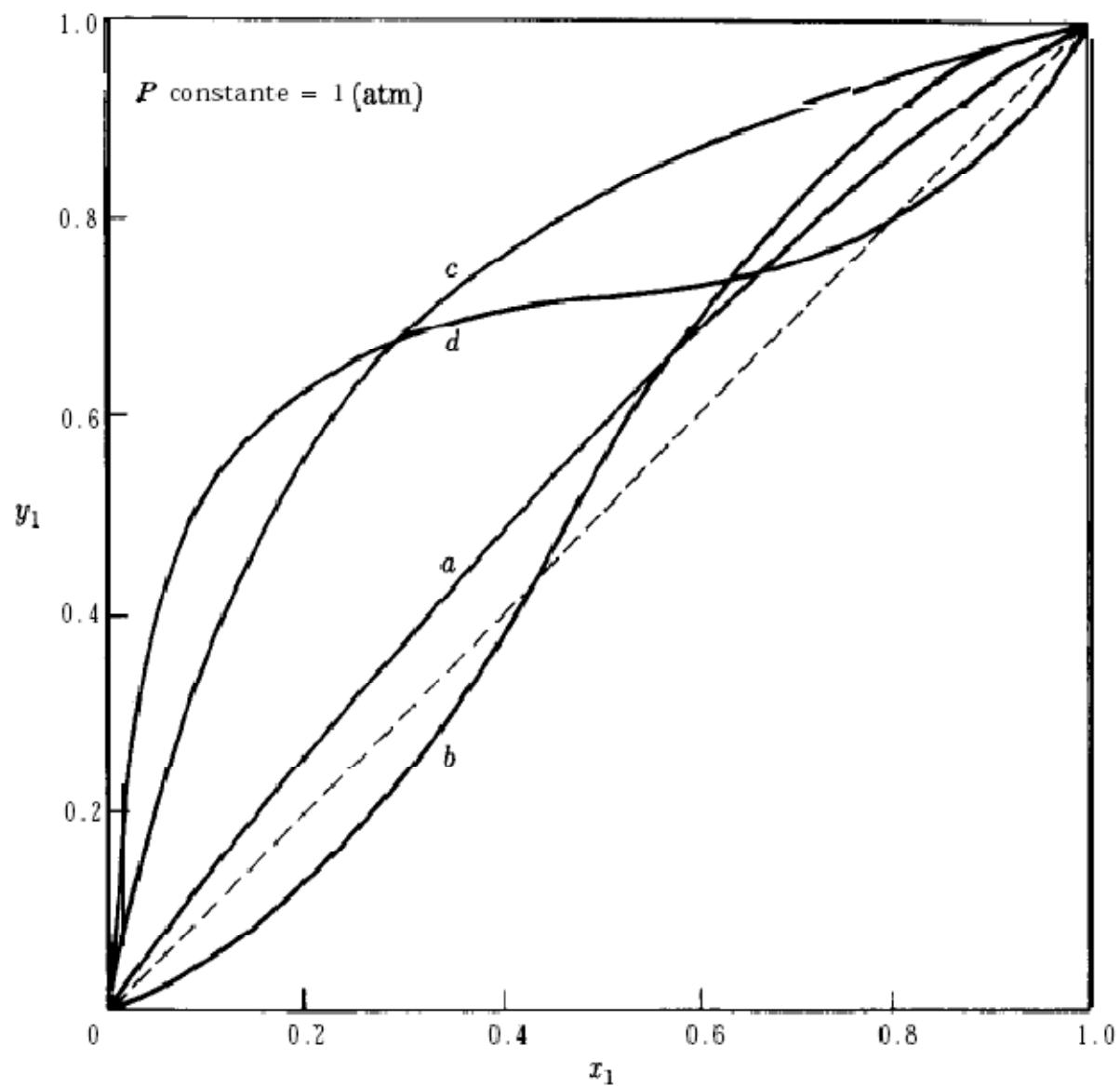


c)



d)

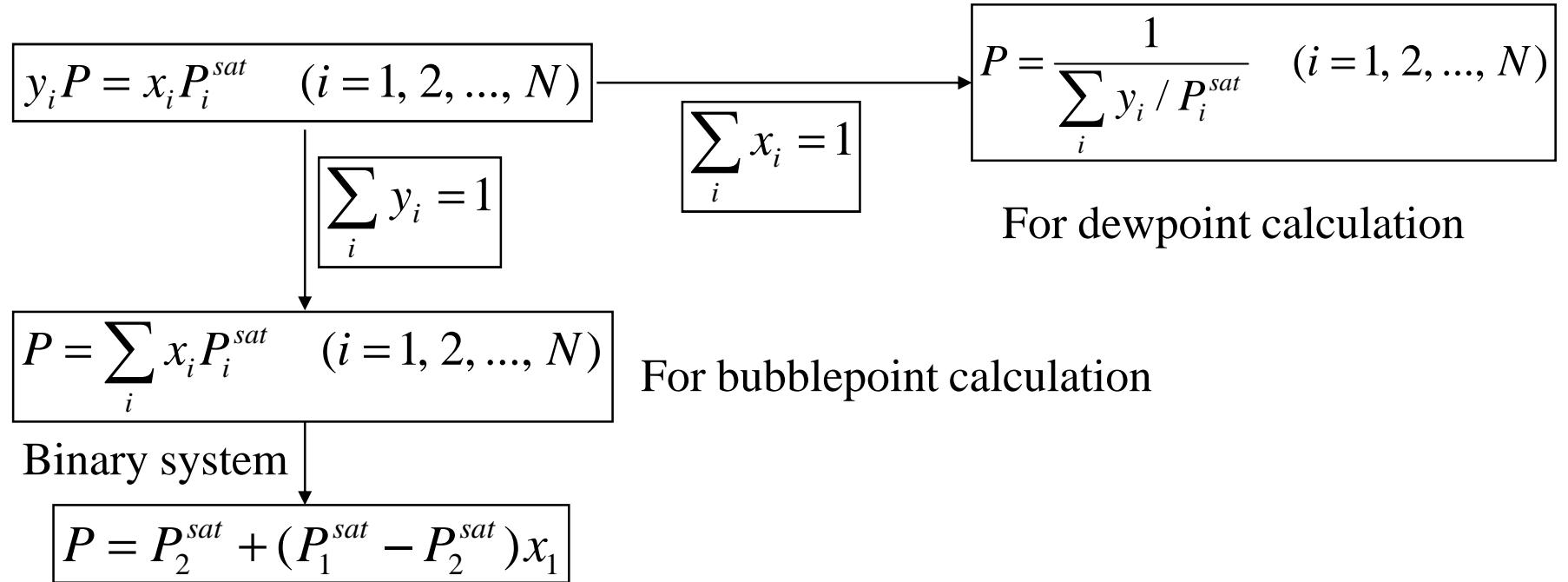
- (a) tetrahydrofuran(1)/ carbon tetrachloride(2)
- (b) Chloroform(1) // tetrahydrofuran(2)
- (c) Furan(1)/ carbon tetrachloride(2)
- (d) Ethanol(1)/ toluene(2)



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# Simple models for VLE

- The simplest are Raoult's law and Henry's law.
- Raoult's law:
  - the vapor phase is an ideal gas (apply for low to moderate pressure)
  - the liquid phase is an ideal solution (apply when the species that are chemically similar)
  - $y_i P = x_i P_i^{sat} \quad (i = 1, 2, \dots, N)$ 
    - although it provides a realistic description of actual behavior for a small class of systems, it is valid for any species present at a mole fraction approaching unity, provided that the vapor phase is an ideal gas.



Binary system acetonitrile (1)/nitromethane(2) conforms closely to Raoult's law. Vapor pressures for the pure species are given by the following Antoine equations:

$$\ln P_1^{sat} / kPa = 14.2724 - \frac{2945.47}{t / ^\circ C + 224.00}$$

$$\ln P_2^{sat} / kPa = 14.2043 - \frac{2972.64}{t / ^\circ C + 209.00}$$

- (a) Prepare a graph showing  $P$  vs.  $x_1$  and  $P$  vs.  $y_1$  for a temperature of  $75^\circ C$ .
  - (b) Prepare a graph showing  $t$  vs.  $x_1$  and  $t$  vs.  $y_1$  for a pressure of 70 kPa.
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(a) BUBL  $P$  
$$P = P_2^{sat} + (P_1^{sat} - P_2^{sat})x_1$$

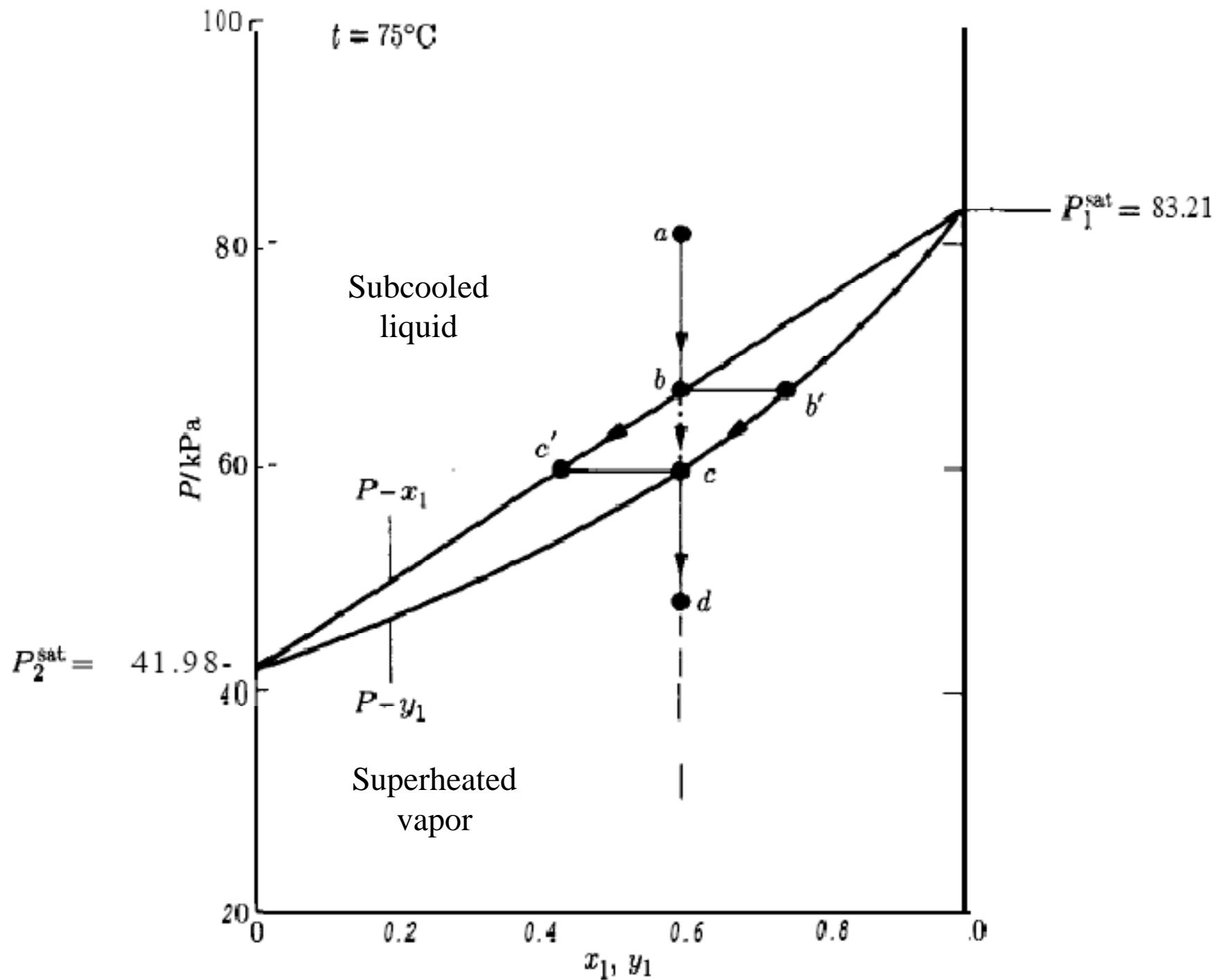
At  $75^\circ C$

$$P_1^{sat} = 83.21$$

$$P_2^{sat} = 41.98$$

$$P = 41.98 + (83.21 - 41.98)x_1 \quad \begin{matrix} \text{e.g. } x_1 = 0.6 \\ P = 66.72 \end{matrix} \rightarrow y_1 = \frac{x_1 P_1^{sat}}{P} = \frac{(0.6)(83.21)}{66.72} = 0.7483$$

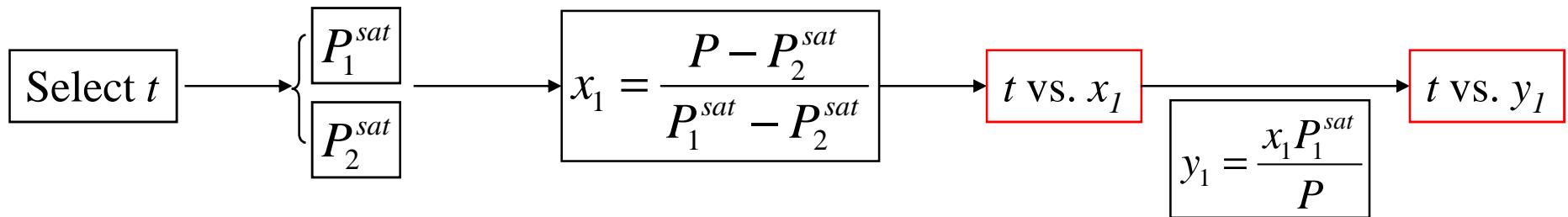
At  $75^\circ C$ , a liquid mixture of 60 mol-% (1) and 40 mol-% (2) is in equilibrium with a vapor containing 74.83 mol-% (1) at pressure of 66.72 kPa.

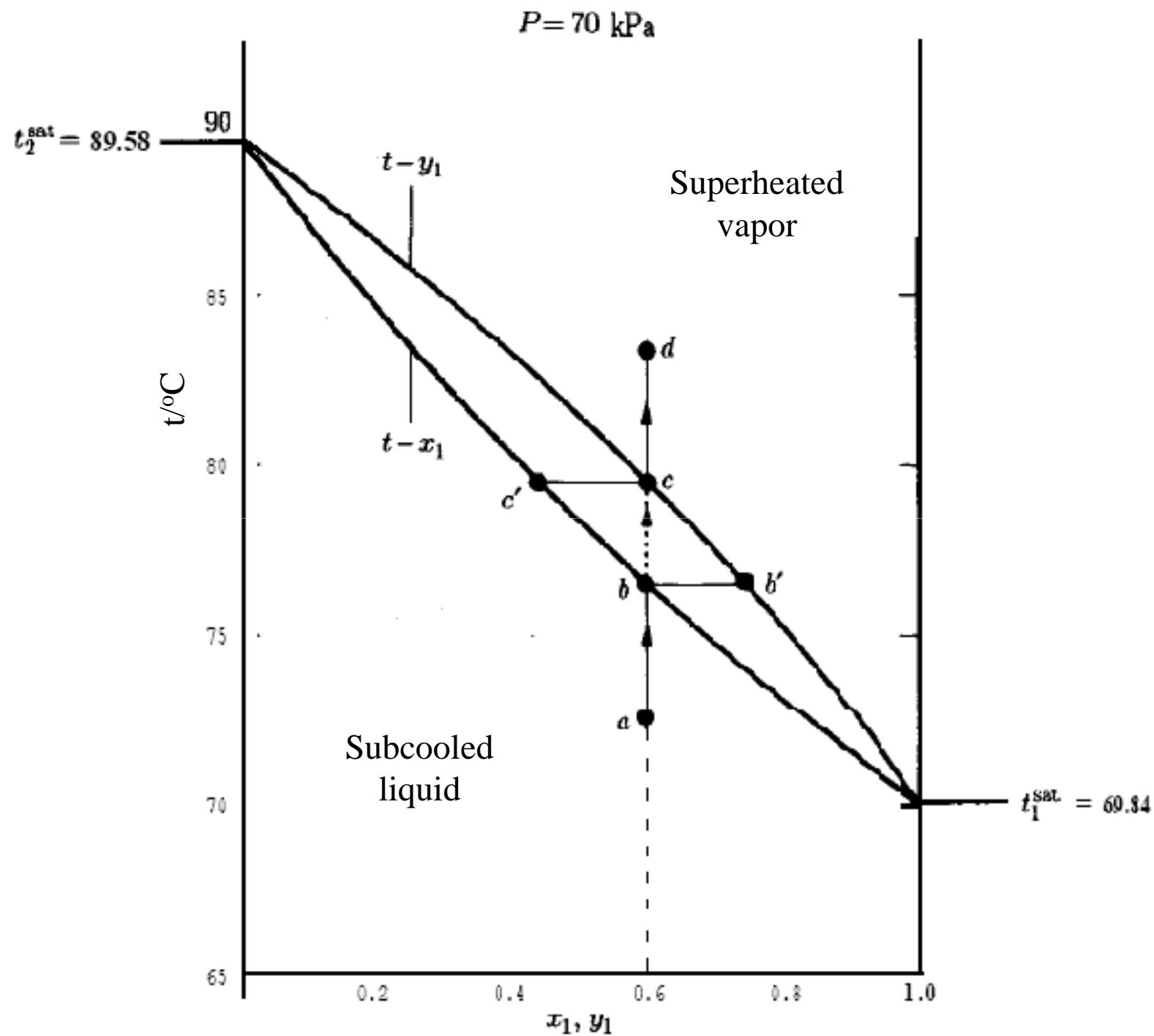


(b) *BUBL T*, having  $P = 70 \text{ kPa}$

$$\ln P_1^{sat} / \text{kPa} = 14.2724 - \frac{2945.47}{t / {}^\circ \text{C} + 224.00}$$

$$\ln P_2^{sat} / \text{kPa} = 14.2043 - \frac{2972.64}{t / {}^\circ \text{C} + 209.00}$$





# Henry's law

- For a species present as a very dilute solute in the liquid phase, the partial pressure of the species in the vapor phase is directly proportional to its liquid-phase mole fraction:

$$y_i P = x_i H_i$$

- $H$  = Henry's Constant
- See table 10.1

Assuming that carbonated water contains only CO<sub>2</sub> (species 1) and H<sub>2</sub>O (species 2), determine the compositions of the vapor and liquid phases in a sealed can of “soda” and the pressure exerted on the can at 10°C. Henry’s constant for CO<sub>2</sub> in water at 10°C is about 990 bar.

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Henry’s law for species 1:

$$y_1 P = x_1 H_1$$

Raoult’s law for species 2:

$$y_2 P = x_2 P_2^{sat}$$

$$P = x_1 H_1 + x_2 P_2^{sat}$$

Assuming x<sub>1</sub> = 0.01

$$P = (0.01)(990) + (0.99)(0.01227) = 9.912$$

$$y_1 P = x_1 H_1 \text{ assuming } y_1 = 1.0$$

Justified the assumption

$$x_1 = 0.01$$

$$y_2 P = x_2 P_2^{sat}$$

$$y_2 = 0.0012$$

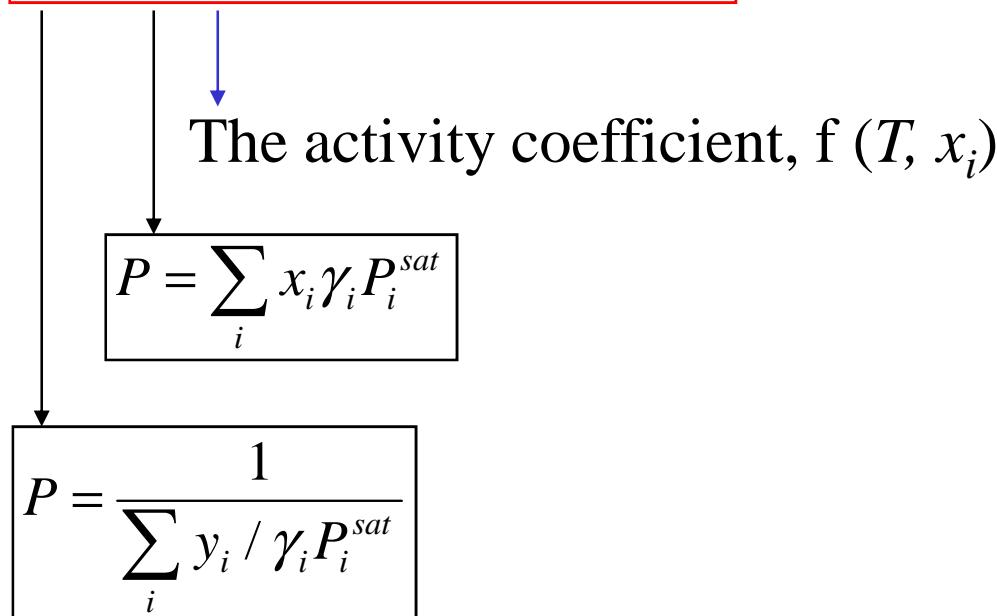
$$y_1 = 0.9988$$

Justified the assumption

# VLE modified Raoult's law

- Account is taken of deviation from solution ideality in the liquid phase by a factor inserted into Raoult's law:

$$y_i P = x_i \gamma_i P_i^{sat} \quad (i = 1, 2, 3, \dots N)$$



For the system methanol (1)/methyl acetate (2), the following equations provide a reasonable correlation for the activity coefficients:

$$\ln \gamma_1 = (2.771 - 0.00523T)x_2^2$$

$$\ln \gamma_2 = (2.771 - 0.00523T)x_1^2$$

The Antoine equations provide vapor pressures:

$$\ln P_1^{sat} / kPa = 16.59158 - \frac{3643.31}{T(K) - 33.424}$$

$$\ln P_2^{sat} / kPa = 14.25326 - \frac{2665.54}{T(K) - 53.424}$$

Calculate

- (a): P and {y<sub>i</sub>} for T = 318.15 K and x<sub>1</sub> = 0.25
  - (b): P and {x<sub>i</sub>} for T = 318.15 K and y<sub>1</sub> = 0.60
  - (c): T and {y<sub>i</sub>} for P = 101.33 kPa and x<sub>1</sub> = 0.85
  - (d): T and {x<sub>i</sub>} for P = 101.33 kPa and y<sub>1</sub> = 0.40
  - (e): the azeotropic pressure and the azeotropic composition for T = 318.15 K
- 

- (a) for T = 318.15, and x<sub>1</sub> = 0.25

$$P_1^{sat} = 44.51 \quad P_2^{sat} = 65.64 \quad \gamma_1 = 1.864 \quad \gamma_2 = 1.072$$

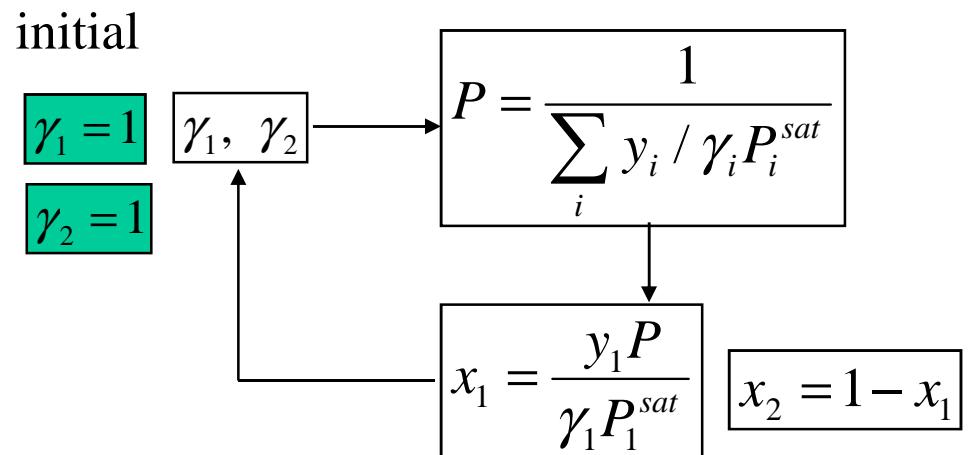
$$P = \sum_i x_i \gamma_i P_i^{sat} = (0.25)(1.864)(44.51) + (0.75)(1.072)(65.64) = 73.50$$

$$y_i P = x_i \gamma_i P_i^{sat} \rightarrow y_1 = 0.282 \quad y_2 = 0.718$$

(b): for  $T = 318.15 \text{ K}$  and  $y_1 = 0.60$

$$P_1^{sat} = 44.51 \quad P_2^{sat} = 65.64$$

A iterative process is applied, with



Converges at:  $P = 62.89 \text{ kPa}$   $y_1 = 1.0378$   $y_2 = 2.0935$   $x_1 = 0.8169$

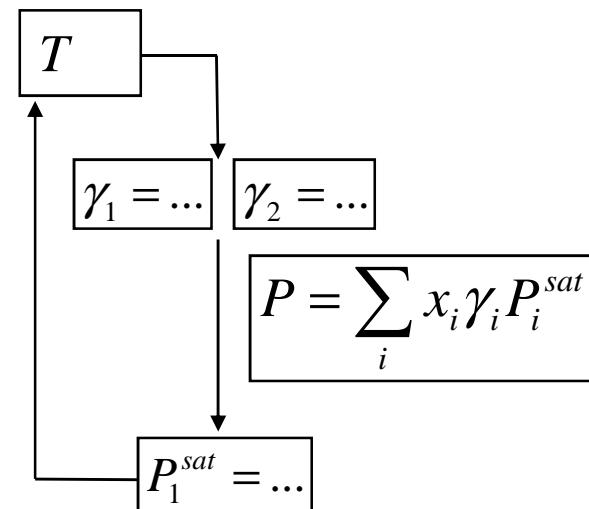
(c): for  $P = 101.33 \text{ kPa}$  and  $x_1 = 0.85$

$$T_1^{sat} = 337.71 \quad T_2^{sat} = 330.08$$

$$T = (0.85)T_1^{sat} + (0.15)T_2^{sat} = 336.57 \quad \text{initial}$$

A iterative process is applied, with

$$\ln P_1^{sat} / \text{kPa} = 16.59158 - \frac{3643.31}{T(K) - 33.424}$$



Converges at:  $T = 331.20 \text{ K}$   $\gamma_1 = 1.0236$   $\gamma_2 = 2.1182$   $y_1 = 0.670$   $y_2 = 0.330$

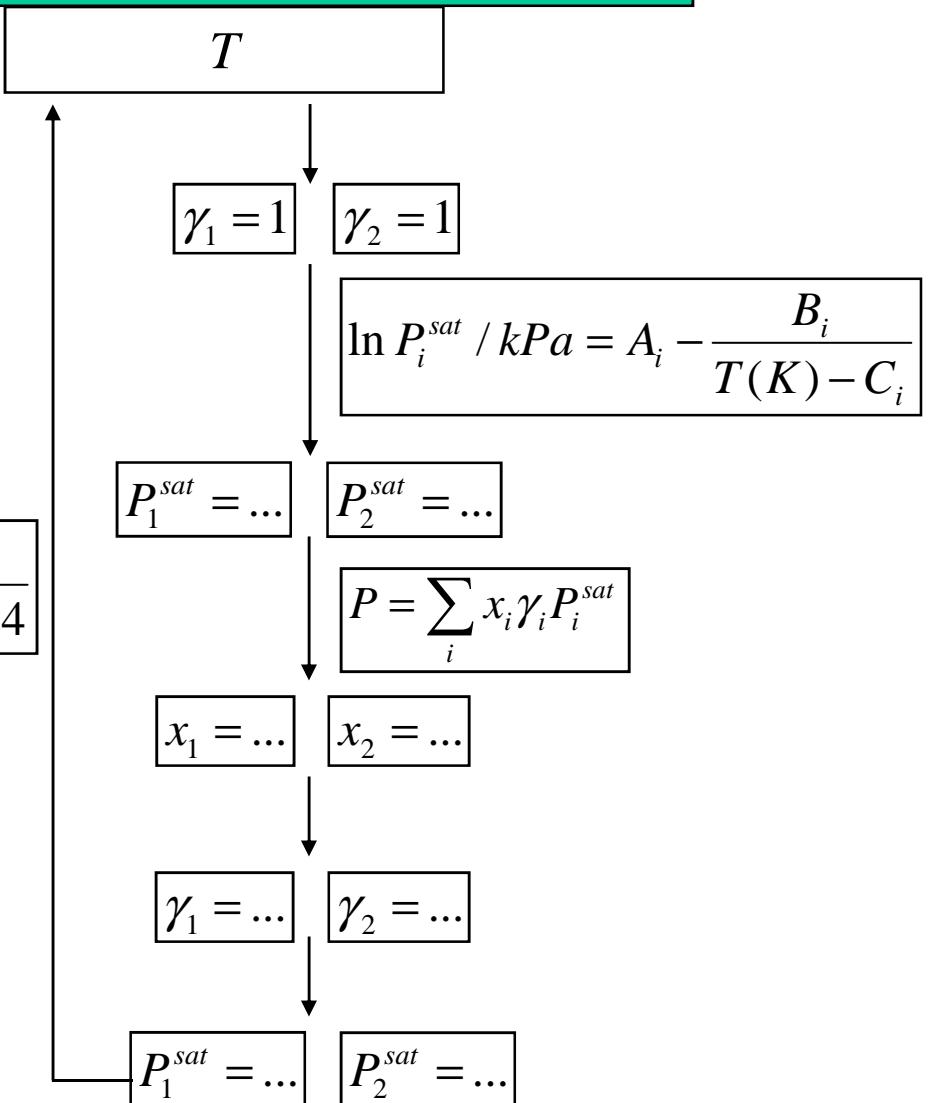
(d): for  $P = 101.33 \text{ kPa}$  and  $y_1 = 0.40$

$$T_1^{sat} = 337.71 \quad T_2^{sat} = 330.08$$

$$T = (0.40)T_1^{sat} + (0.60)T_2^{sat} = 333.13 \quad \text{initial}$$

A iterative process is applied, with

$$\ln P_1^{sat} / \text{kPa} = 16.59158 - \frac{3643.31}{T(K) - 33.424}$$



Converges at:  $T = 326.70 \text{ K}$     $\gamma_1 = 1.3629$     $\gamma_2 = 1.2523$     $x_1 = 0.4602$     $x_2 = 0.5398$

(e): the azeotropic pressure and the azeotropic composition for T = 318.15 K

Define the relative volatility:

$$\alpha_{12} \equiv \frac{\frac{y_1}{x_1}}{\frac{y_2}{x_2}} \xrightarrow{y_i P = x_i \gamma_i P_i^{sat}} \alpha_{12} = \frac{\gamma_1 P_1^{sat}}{\gamma_2 P_2^{sat}}$$

Azeotrope  $\longrightarrow y_1 = x_1 \quad y_2 = x_2 \longrightarrow \alpha_{12} = 1$

$$\alpha_{12} \Big|_{x_1=0} = \frac{P_1^{sat} \exp(2.771 - 0.00523T)}{P_2^{sat}} = 2.052 \quad \alpha_{12} \Big|_{x_1=1} = \frac{P_1^{sat}}{P_2^{sat} \exp(2.771 - 0.00523T)} = 0.224$$

Since  $\alpha_{12}$  is a continuous function of  $x_1$ : from 2.052 to 0.224,  $\alpha_{12} = 1$  at some point

**There exists the azeotrope!**

$$\alpha_{12} = \frac{\gamma_1 P_1^{sat}}{\gamma_2 P_2^{sat}} = 1 \longrightarrow \frac{\gamma_1^{az}}{\gamma_2^{az}} = \frac{P_2^{sat}}{P_1^{sat}} = 1.4747$$

$$\left. \begin{array}{l} \ln \gamma_1 = (2.771 - 0.00523T)x_2^2 \\ \ln \gamma_2 = (2.771 - 0.00523T)x_1^2 \end{array} \right\}$$

$$\ln \frac{\gamma_1}{\gamma_2} = (2.771 - 0.00523T)(x_2 - x_1) = (2.771 - 0.00523T)(1 - 2x_1)$$

$$x_1^{az} = 0.325 = y_1^{az} \longrightarrow \gamma_1^{az} = 1.657$$

$$P^{az} = \gamma_1^{az} P_1^{sat} = 73.76 \text{ kPa}$$

# VLE from K-value correlations

- A convenient measure, the *K-value*:

$$K_i \equiv \frac{y_i}{x_i}$$

- the “lightness” of a constituent species, i.e., of its tendency to favor the vapor phase.

- The Raoult’s law:

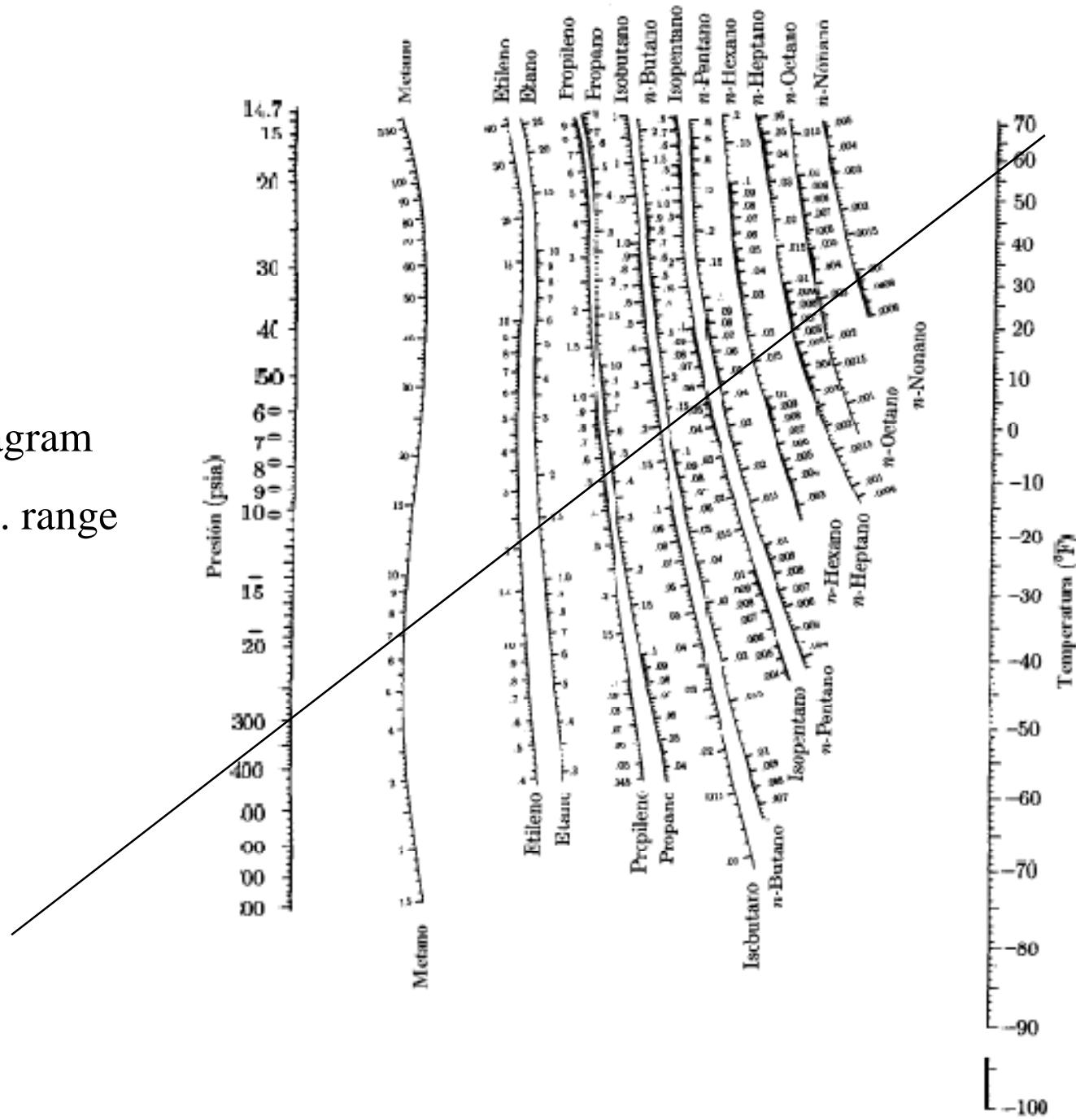
$$K_i = \frac{P_i^{sat}}{P}$$

- The modified Raoult’s law:

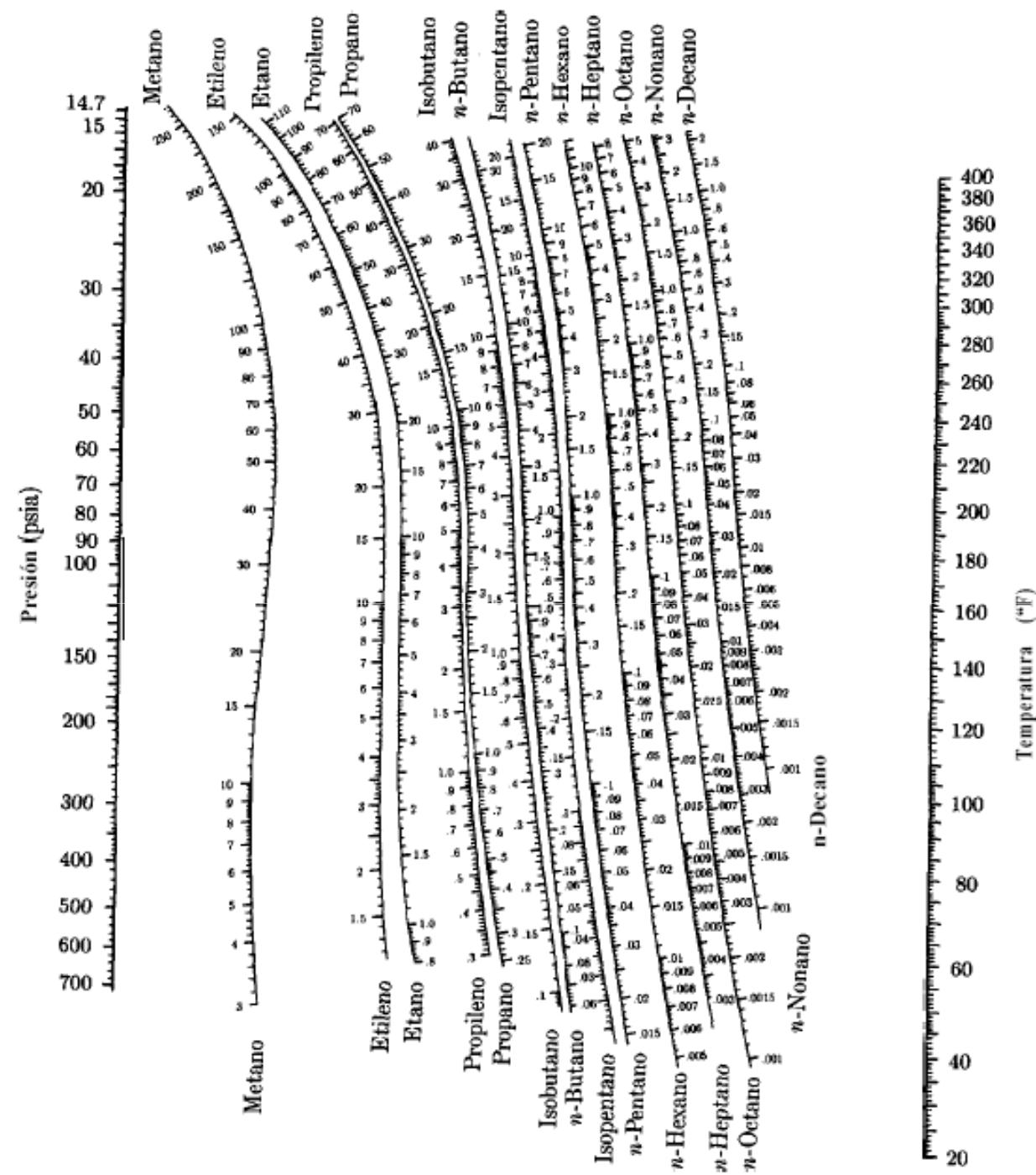
$$K_i = \frac{\gamma_i P_i^{sat}}{P}$$

# De Priester Diagram

## For Low-Temp. range



## De Priester's Diagram for High-Temp. range



For a mixture of 10 mol-% methane, 20 mol-% ethane, and 70 mol-% propane at 50°F, determine: (a) the dewpoint pressure, (b) the bubblepoint pressure. The K-values are given by Fig. 10.13.

(a) at its dewpoint, only an insignificant amount of liquid is present:

|         |       | $P = 100 \text{ (psia)}$   |             | $P = 150 \text{ (psia)}$   |             | $P = 126 \text{ (psia)}$   |             |
|---------|-------|----------------------------|-------------|----------------------------|-------------|----------------------------|-------------|
| Species | $y_i$ | $K_i$                      | $y_i / K_i$ | $K_i$                      | $y_i / K_i$ | $K_i$                      | $y_i / K_i$ |
| Methane | 0.10  | 20.0                       | 0.005       | 13.2                       | 0.008       | 16.0                       | 0.006       |
| Ethane  | 0.20  | 3.25                       | 0.062       | 2.25                       | 0.089       | 2.65                       | 0.075       |
| Propane | 0.70  | 0.92                       | 0.761       | 0.65                       | 1.077       | 0.762                      | 0.919       |
|         |       | $\sum (y_i / K_i) = 0.828$ |             | $\sum (y_i / K_i) = 1.174$ |             | $\sum (y_i / K_i) = 1.000$ |             |



(b) at bubblepoint, the system is almost completely condensed:

|         |       | $P = 380 \text{ (psia)}$ |           | $P = 400 \text{ (psia)}$ |           | $P = 385 \text{ (psia)}$ |           |
|---------|-------|--------------------------|-----------|--------------------------|-----------|--------------------------|-----------|
| Species | $x_i$ | $K_i$                    | $x_i K_i$ | $K_i$                    | $x_i K_i$ | $K_i$                    | $x_i K_i$ |
| Methane | 0.10  | 5.60                     | 0.560     | 5.25                     | 0.525     | 5.49                     | 0.549     |
| Ethane  | 0.20  | 1.11                     | 0.222     | 1.07                     | 0.214     | 1.10                     | 0.220     |
| Propane | 0.70  | 0.335                    | 0.235     | 0.32                     | 0.224     | 0.33                     | 0.231     |
|         |       | $\sum (x_i K_i) = 1.017$ |           | $\sum (x_i K_i) = 0.963$ |           | $\sum (x_i K_i) = 1.000$ |           |



# Flash calculations

- A liquid at a pressure equal to or greater than its bubblepoint pressure “flashes” or partially evaporates when the pressure is reduced, producing a two-phase system of vapor and liquid in equilibrium.
- Consider a system containing one mole of nonreacting chemical species:

$$\begin{array}{c} L + V = 1 \\ \downarrow \quad \downarrow \\ \text{The moles of liquid} \end{array} \quad \begin{array}{c} z_i = x_i L + y_i V \\ \downarrow \quad \downarrow \\ \text{The liquid mole fraction} \end{array} \quad \begin{array}{c} z_i = x_i(1 - V) + y_i V \\ \downarrow \\ \begin{array}{c} y_i = \frac{z_i K_i}{1 + V(K_i - 1)} \\ \downarrow \\ \sum \frac{z_i K_i}{1 + V(K_i - 1)} = 1 \end{array} \end{array}$$

The system acetone (1)/acetonitrile (2)/nitromethane(3) at 80°C and 110 kPa has the overall composition,  $z_1 = 0.45$ ,  $z_2 = 0.35$ ,  $z_3 = 0.20$ , Assuming that Raoult's law is appropriate to this system, determine L, V,  $\{x_i\}$ , and  $\{y_i\}$ . The vapor pressures of the pure species are given.

Do a *BUBL P* calculation, with  $\{z_i\} = \{x_i\}$  :

$$P_{\text{bUBL}} = x_1 P_1^{\text{sat}} + x_2 P_2^{\text{sat}} + x_3 P_3^{\text{sat}} = (0.45)(195.75) + (0.35)(97.84) + (0.20)(50.32) = 132.40 \text{ kPa}$$

Do a *DEW P* calculation, with  $\{z_i\} = \{y_i\}$  :

$$P_{\text{dew}} = \frac{1}{y_1 / P_1^{\text{sat}} + y_2 / P_2^{\text{sat}} + y_3 / P_3^{\text{sat}}} = 101.52 \text{ kPa}$$

$$L = 1 - V = 0.2636 \text{ mol}$$

Since  $P_{\text{dew}} < P = 110 \text{ kPa} < P_{\text{bUBL}}$ , the system is in the two-phase region,

$$K_i = \frac{P_i^{\text{sat}}}{P}$$

$$K_1 = 1.7795$$

$$K_2 = 0.8895$$

$$K_3 = 0.4575$$

$$\sum \frac{z_i K_i}{1 + V(K_i - 1)} = 1$$

$$V = 0.7364 \text{ mol}$$

$$y_i = \frac{z_i K_i}{1 + V(K_i - 1)}$$

$$x_1 = 0.2859$$

$$x_2 = 0.3810$$

$$x_3 = 0.3331$$

$$K_i \equiv \frac{y_i}{x_i}$$

$$y_1 = 0.5087$$

$$y_2 = 0.3389$$

$$y_3 = 0.1524$$