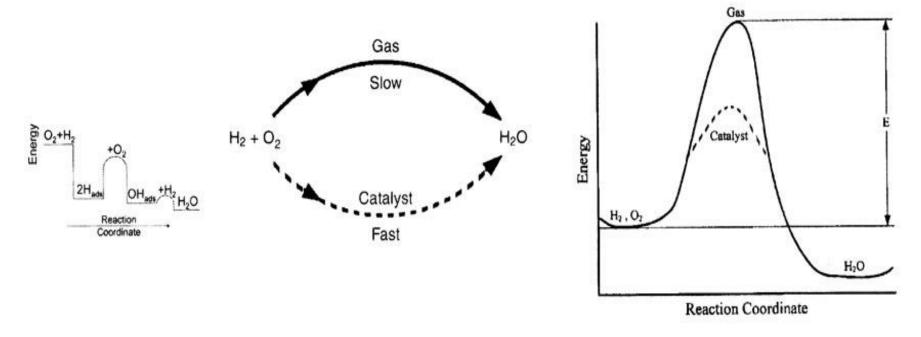
# Catalysis and Catalytic Reactors

Fogler-Chapter 10

- A Catalyst is a substance that affects the rate of chemical reaction but emerges from the process unchanged.
- Catalysis is the occurrence, study, and use of catalysts and catalytic processes.

Approximately 1/3 of the GNP of materials produced in the U.S. involves a catalytic process.

Catalysts affect both selectivity and yield



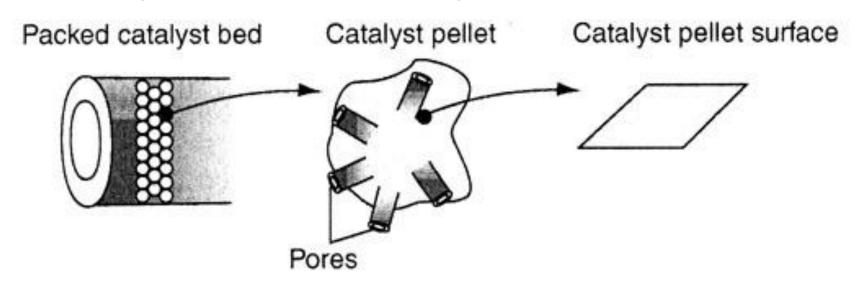
Different reaction paths



#### Different shapes and sizes of catalyst.

Material aktif = katalis

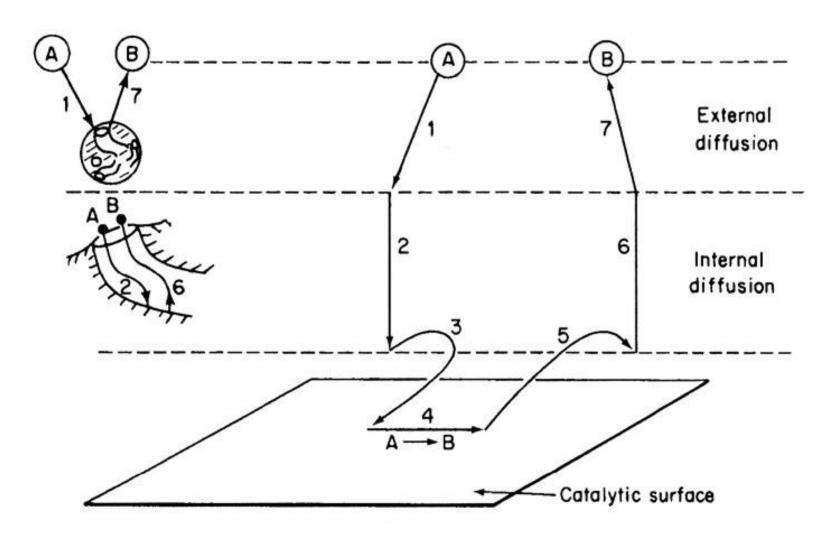
Support= Material yang tidak aktif tetapi dijadikan tempat menempel katalis Promoter= Sejumlah kecil aktif material tambahan yang meningkatkan aktivitas katalis



Catalytic packed-bed reactor, schematic.



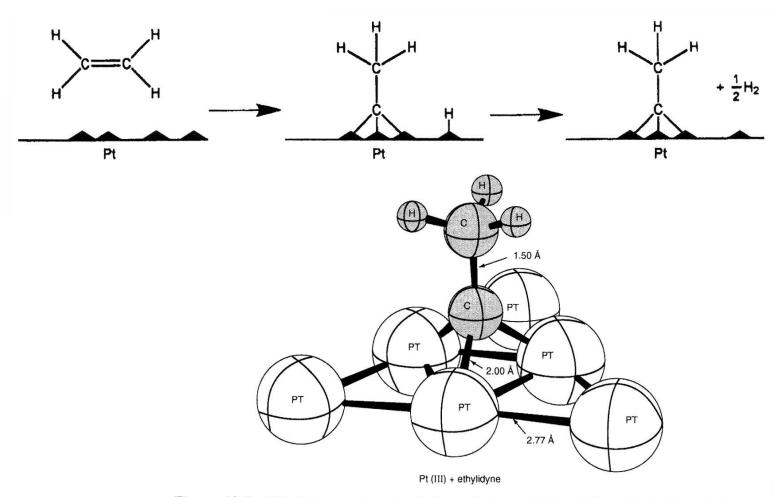
# Steps in a Catalytic Reaction



#### **Active Sites**

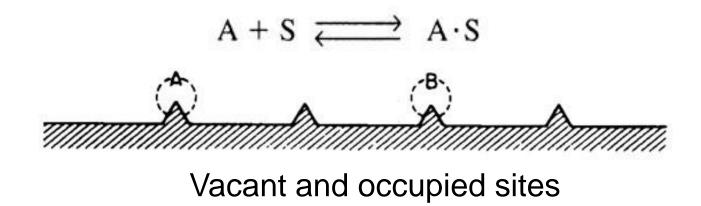
- Reactions are not catalyzed over the entire surface but only at certain active sites or centers that result from unsaturated atoms in the surface.
- An active site is a point on the surface that can form strong chemical bonds with an adsorbed atom or molecule.

# Active Sites – Ethylidyne on Platinum



**Figure 10-3** Ethylidyne as chemisorbed on platinum. (Adapted from G. A. Somorjai, *Introduction to Surface Chemistry and Catalysis*, Wiley, New York, 1994.)

#### The Adsorption Step



For the system shown, the total concentration of sites is

$$C_t = C_v + C_{A.S} + C_{B.S}$$

# The Adsorption Step

$$A + S \leftrightarrow A \bullet S$$

$$r_{AD} = k_A P_A C_v - k_{-A} C_{A \bullet S} = k_A \left[ P_A C_V - C_{A \bullet S} / K_A \right]$$
$$K_A = k_A / k_{-A} \quad \text{[atm}^{-1}\text{]}$$

@ equilibrium : 
$$r_{AD} = 0$$
 
$$C_{AS} = k_A P_A C_V$$
 
$$r_{AD} / k_A \approx 0 \qquad C_{AS} = k_A P_A C_V$$

$$C_{t} = C_{V} + C_{A \bullet S} = C_{V} + K_{A} P_{A} C_{V} = C_{V} (1 + K_{A} P_{A})$$

$$C_{V} = \frac{C_{t}}{1 + K_{A} P_{A} C_{V}}$$

# Langmuir Adsorption Isotherm

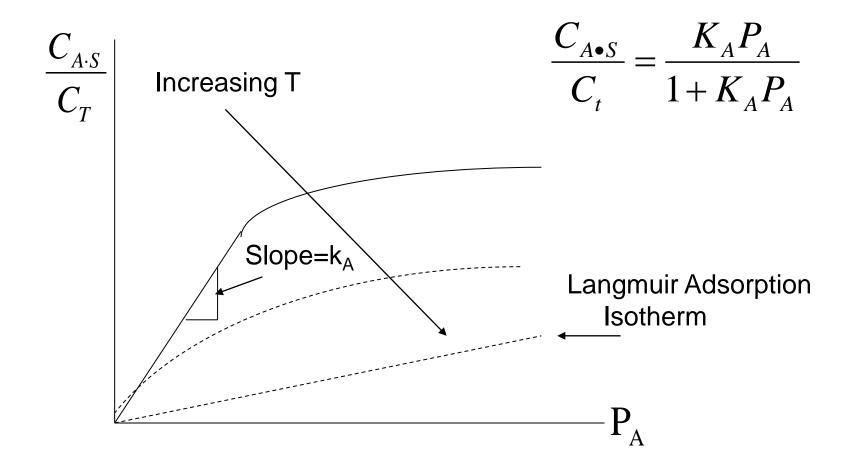
$$C_V = \frac{C_t}{1 + K_A P_A C_V}$$

$$C_{A\bullet S}=K_AP_AC_V$$

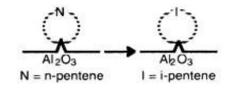
$$C_{A \bullet S} = \frac{K_A P_A}{1 + K_A P_A} C_t$$

$$\frac{C_{A \bullet S}}{C_t} = \frac{K_A P_A}{1 + K_A P_A}$$

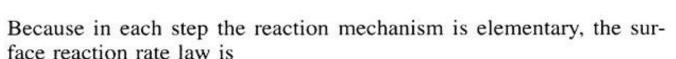
# Langmuir Adsorption Isotherm



 Single site. The surface reaction may be a single-site mechanism in which only the site on which the reactant is adsorbed is involved in the reaction. For example, an adsorbed molecule of A may isomerize (or perhaps decompose) directly on the site to which it is attached, such as



$$A \cdot S \iff B \cdot S$$



Single Site

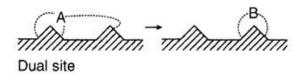
$$k_{\rm S} = \left(\frac{1}{\rm s}\right)$$

 $K_s = (dimensionless)$ 

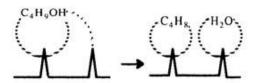
$$r_{\rm S} = k_{\rm S} \left( C_{\rm A \cdot S} - \frac{C_{\rm B \cdot S}}{K_{\rm S}} \right)$$

where  $K_S$  is the surface reaction equilibrium constant  $K_S = k_S/k_{-S}$ 

 Dual site. The surface reaction may be a dual-site mechanism in which the adsorbed reactant interacts with another site (either unoccupied or occupied) to form the product.



For example, adsorbed A may react with an adjacent vacant site to yield a vacant site and a site on which the product is adsorbed, such as the dehydration of butanol.



For the generic reaction

$$A \cdot S + S \longrightarrow B \cdot S + S$$

the corresponding surface reaction rate law is

$$r_{\rm S} = k_{\rm S} \left( C_{\rm A \cdot S} C_v - \frac{C_{\rm B \cdot S} C_v}{K_{\rm S}} \right) \tag{10-}$$

Dual Site

$$r_{\rm S} = \left(\frac{\rm mol}{\rm gcat} \cdot {\rm s}\right)$$

$$k_{\rm S} = \left(\frac{\rm gcat}{\rm mol \cdot s}\right)$$

$$K_S = (dimensionless)$$

the corresponding surface reaction rate law is

$$r_{\rm S} = k_{\rm S} \left( C_{\rm A \cdot S} C_v - \frac{C_{\rm B \cdot S} C_v}{K_{\rm S}} \right)$$

Another example of a dual-site mechanism is the reaction between two adsorbed species, such as the reaction of CO with O

For the generic reaction

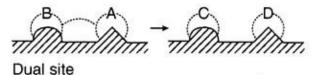
$$A \cdot S + B \cdot S \iff C \cdot S + D \cdot S$$

the corresponding surface reaction rate law is

$$r_{\rm S} = k_{\rm S} \left( C_{\rm A \cdot S} C_{\rm B \cdot S} - \frac{C_{\rm C \cdot S} C_{\rm D \cdot S}}{K_{\rm S}} \right)$$

A third dual-site mechanism is the reaction of two species adsorbed on different types of sites S and S', such as the reaction of CO with O.

For the generic reaction



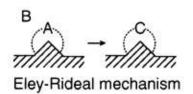
$$A \cdot S + B \cdot S' \iff C \cdot S' + D \cdot S$$

the corresponding surface reaction rate law is

$$r_{\rm S} = k_{\rm S} \left( C_{\rm A \cdot S} C_{\rm B \cdot S'} - \frac{C_{\rm C \cdot S'} C_{\rm D \cdot S}}{K_{\rm S}} \right)$$

Langmuir-Hinshelwood kinetics Reactions involving either single- or dual-site mechanisms, which were described earlier are sometimes referred to as following *Lang-muir–Hinshelwood kinetics*.

 Eley-Rideal. A third mechanism is the reaction between an adsorbed molecule and a molecule in the gas phase, such as the reaction of propylene and benzene





For the generic reaction

$$A \cdot S + B(g) \iff C \cdot S$$

the corresponding surface reaction rate law is

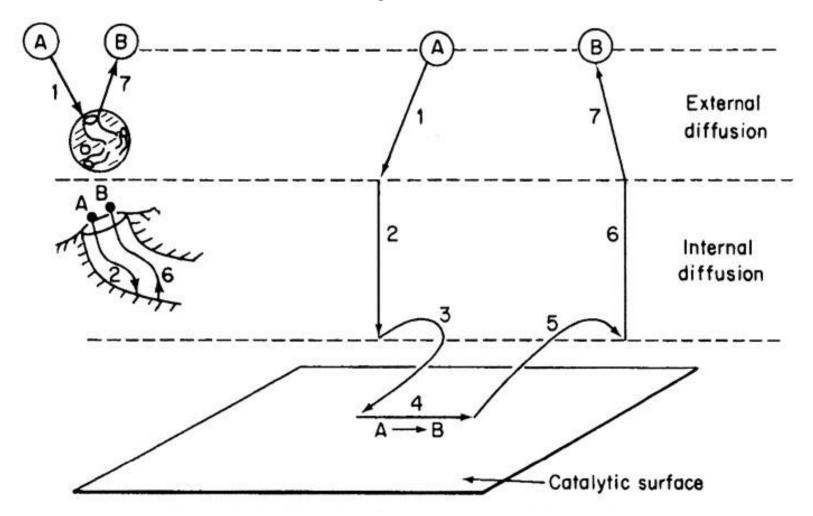
$$r_{\rm S} = k_{\rm S} \left( C_{\rm A \cdot S} P_{\rm B} - \frac{C_{\rm C \cdot S}}{K_{\rm S}} \right)$$

This type of mechanism is referred to as an *Eley-Rideal mechanism*.

$$k_{\rm s} = \left(\frac{1}{\rm atm \cdot s}\right)$$

$$K_{\rm S} = \left(\frac{1}{\rm atm}\right)$$

# Steps in a Catalytic Reaction



#### Desorption from the Surface for the Reaction

$$r_{DC} = k_D \left| C_{C \bullet S} - \frac{P_C C_{\upsilon}}{K_{DC}} \right|$$
 (10-20)

$$r_{DC} = -r_{ADC}$$

$$K_{DC} = \frac{1}{K_C}$$

$$r_{DC} = k_D \left[ C_{C \bullet S} - K_C P_C C_{\upsilon} \right]$$

(10-21)

#### Steps in a Single-Site Catalytic Reactor

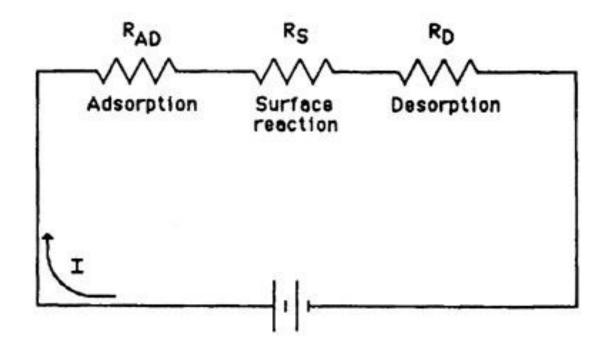
Adsorption  $A + S \leftrightarrow A \bullet S - r_A = r_{Ad} = k_{Ad} \left| P_A C_v - \frac{C_{A \bullet S}}{k_A} \right|$ 

Surface Reaction  $A \bullet S \leftrightarrow B \bullet S$   $-r_A = r_S = k_S \left[ C_{A \bullet S} - \frac{C_{B \bullet S}}{k_C} \right]$ 

Desorption  $B \bullet S \longleftrightarrow B + S - r_A = r_D = k_D [C_{B \bullet S} - k_B P_B C_B]$ 

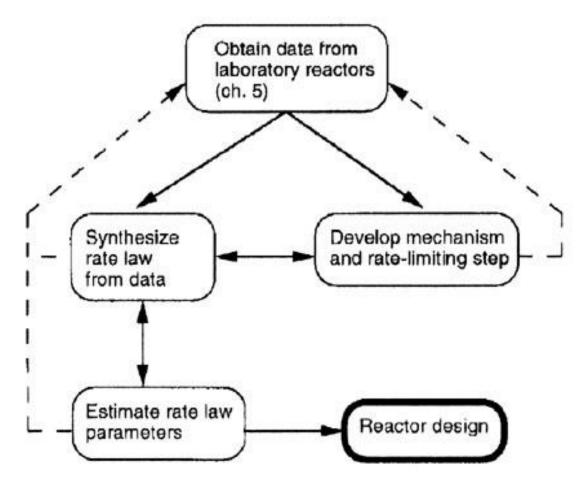
Which step is the Rate Limiting Step (RLS)?

# The Rate Limiting Step: Which step has the largest resistance?



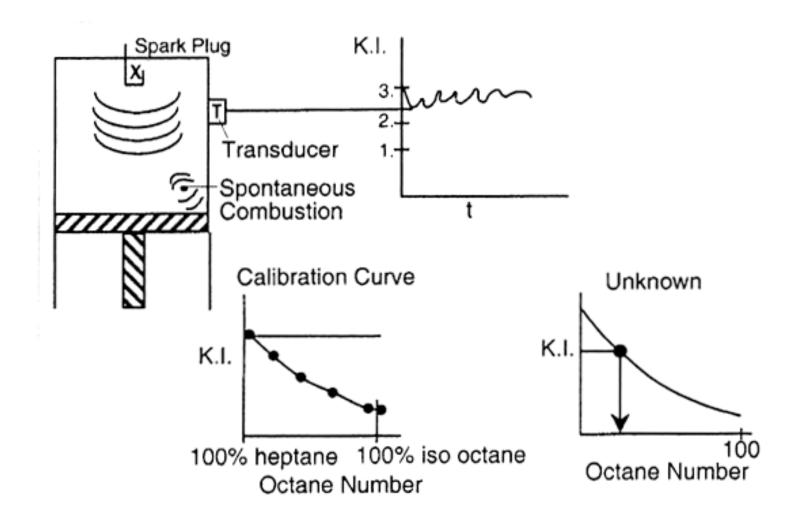
Electrical analog to heterogeneous reactions

# Collecting and Analyzing Data



Collecting information for catalytic reactor design

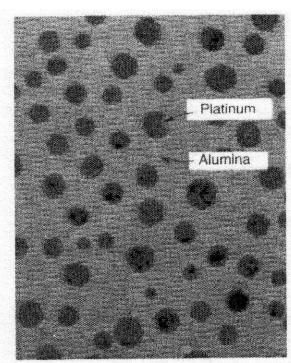
# Collecting and Analyzing Data



- Normal Pentane Octane Number = 62
- Iso-Pentane Octane Number = 95

#### Gasoline

$C_5$	10%		
C <sub>6</sub>	10%		
C <sub>7</sub>	20%		
C <sub>8</sub>	25%		
C <sub>9</sub>	20%		
C <sub>10</sub>	10%		
C11-12	5%		



Platinum on alumina. (Figure from R.I. Masel, *Chemical Kinetics and Catalysis*, Wiley, New York, 2001, p. 700)

*n*-pentane 
$$0.75 \text{ wt\% Pt} \atop \leftarrow Al_2O_3$$
 *i*-pentane

*n*-pentene 
$$\xrightarrow{Al_2O_3}$$
 *i*-pentene

$$\mathsf{N} \stackrel{\longrightarrow}{\longleftarrow} \mathsf{I}$$

Isomerization of *n*-pentene (N) to *i*-pentene (I) over alumina

$$N \quad \stackrel{\mathsf{Al_2O_3}}{\longleftarrow} \quad \mathsf{I}$$

1. Select a mechanism (Mechanism Single Site)

Adsorption on Surface:  $N + S \Leftrightarrow N \bullet S$ 

Surface Reaction:  $N \bullet S \Leftrightarrow I \bullet S$ 

Desorption:  $I \bullet S \Leftrightarrow I + S$ 

Treat each reaction step as an elementary reaction when writing rate laws.

#### 2. Assume a rate-limiting step.

Choose the surface reaction first, since more than 75% of all heterogenous reactions that are not diffusion-limited are surface-reaction-limited. The rate law for the surface reaction step is:

$$N \bullet S + S \Leftrightarrow I \bullet S + S$$

$$-r_{N}' = r_{I}' = r_{S} = k_{S} \left( C_{N \bullet S} - \frac{C_{I \bullet S}}{K_{S}} \right)$$

3. Find the expression for the concentrations of the adsorbed species

 $C_{N.S}$  and  $C_{I.S}$ . Use the other steps that are not limiting to solve for  $C_{N.S}$  and  $C_{I.S}$ . For this reaction:

$$N + S \Leftrightarrow N \bullet S$$

From 
$$\frac{r_{AD}}{k_A} \approx 0$$
:  $C_{N \bullet S} = P_N K_N C_v$ 

$$I \bullet S \Leftrightarrow I + S$$

From 
$$\frac{r_D}{k_D} \approx 0$$
:  $C_{I \bullet S} = \frac{P_I C_v}{K_D} = K_I P_I C_v$ 

4. Write a Site Balance.

$$C_{t} = C_{v} + C_{N \bullet S} + C_{I \bullet S}$$

5. Derive the rate law. Combine steps 2, 3 and 4 to arrive at the rate law:

$$-r_{N}' = r_{S} = \frac{k_{S}C_{t}K_{N}(P_{N} - P_{I}/K_{P})}{(1 + K_{N}P_{N} + K_{I}P_{I})}$$

$$-r_{N}' = r_{S} = \frac{k(P_{N} - P_{I}/K_{P})}{(1 + K_{N}P_{N} + K_{I}P_{I})}$$

	1994	2004	2008
HC	0.41	0.125	0.10
CO	3.4	3.4	3.4
NO	0.4	0.4	0.14

$$CO + NO \rightarrow CO_2 + \frac{1}{2}N_2$$

$$NO + S \xrightarrow{\longrightarrow} NO \cdot S$$

$$r_{ANO} = k_{NO} \left[ P_{NO} C_{V} - \frac{C_{NO \cdot S}}{K_{NO}} \right] \quad C_{NO \cdot S} = K_{NO} P_{NO} C_{V}$$

$$CO \cdot S \xrightarrow{\leftarrow} CO \cdot S$$

$$r_{ACO} = k_{CO} \left[ P_{CO} C_{V} - \frac{C_{CO \cdot S}}{K_{CO}} \right] \quad C_{CO \cdot S} = K_{CO} P_{CO} C_{V}$$

$$CO \cdot S + NO \cdot S \rightarrow CO_2 + N \cdot S + S$$
  $r_S = k_S [C_{CO \cdot S} C_{NO \cdot S}]$ 

$$r_{S} = k_{S} \left[ C_{CO \cdot S} C_{NO \cdot S} \right]$$

$$N \cdot S + N \cdot S \xrightarrow{} N_2(g) + 2S$$

$$r_{D} = k_{D} [C_{N-S}^{2} - K_{N_{2}} P_{N_{2}} C_{V}^{2}]$$
  $C_{N-S} = C_{V} \sqrt{K_{N} P_{N_{2}}}$ 

$$C_{N \cdot S} = C_V \sqrt{K_N P_{N_2}}$$

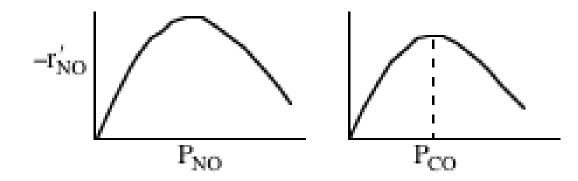
$$\begin{split} r_{S} &= k_{S} \big[ C_{NO \bullet S} C_{CO \bullet S} \big] \\ r_{S} &= k_{S} K_{NO} K_{CO} P_{NO} P_{CO} C_{V}^{2} \\ C_{T} &= C_{V} + C_{NO \bullet S} + C_{CO \bullet S} + C_{N \bullet S} \\ &= C_{V} + C_{V} K_{NO} P_{NO} + C_{V} K_{CO} P_{CO} + C_{V} \sqrt{K_{N_{2}} P_{N_{2}}} \end{split}$$

$$\begin{split} C_{\mathrm{V}} &= \frac{C_{\mathrm{t}}}{1 + K_{\mathrm{NO}} P_{\mathrm{NO}} + K_{\mathrm{CO}} P_{\mathrm{CO}} + \sqrt{K_{\mathrm{N_{2}}} P_{\mathrm{N_{2}}}}} \\ -r_{\mathrm{NO}}' &= r_{\mathrm{S}} = \frac{\frac{k_{\mathrm{S}} K_{\mathrm{NO}} K_{\mathrm{CO}} C_{\mathrm{t}}^{2}}{k_{\mathrm{S}} K_{\mathrm{NO}} K_{\mathrm{CO}} C_{\mathrm{t}}^{2}} P_{\mathrm{NO}} P_{\mathrm{CO}}}{\left(1 + K_{\mathrm{NO}} P_{\mathrm{NO}} + K_{\mathrm{CO}} P_{\mathrm{CO}} + \sqrt{K_{\mathrm{N_{2}}} P_{\mathrm{N_{2}}}}\right)^{2}} \\ -r_{\mathrm{NO}}' &= \frac{k P_{\mathrm{NO}} P_{\mathrm{CO}}}{\left(1 + K_{\mathrm{NO}} P_{\mathrm{NO}} + K_{\mathrm{CO}} P_{\mathrm{CO}} + \sqrt{K_{\mathrm{N_{2}}} P_{\mathrm{N_{2}}}}\right)^{2}} \end{split}$$

$$-r'_{NO} = \frac{kP_{NO}P_{CO}}{\left(1 + K_{NO}P_{NO} + K_{CO}P_{CO} + \sqrt{K_{N_2}P_{N_2}}\right)^2}$$

Neglect  $\sqrt{K_{N_2}P_{N_2}}$ 

$$-r'_{NO} = \frac{kP_{NO}P_{CO}}{(1 + K_{NO}P_{NO} + K_{CO}P_{CO})^{2}}$$



$$-r'_{NO} = \frac{kP_{NO}P_{CO}}{(1 + K_{NO}P_{NO} + K_{CO}P_{CO})^2}$$

Find optimum partial pressure of CO

$$\frac{d(-r_{NO})}{dP_{CO}} = 0$$

$$P_{CO} = \frac{I + K_{NO} P_{NO}}{K_{CO}}$$

$$-r'_{NO}$$