

KK 2916626, Induksi Magnetik



Program Studi : S1 Pendidikan IPA  
FAKULTAS KEGURUAN DAN ILMU  
PENDIDIKAN  
UNIVERSITAS SEBELAS MARET (UNS)  
SURAKARTA

Pertemuan ke-4 (Kelas A) : Selasa, 17 Maret 2020 Pk. 12.40 – 15.00 wib

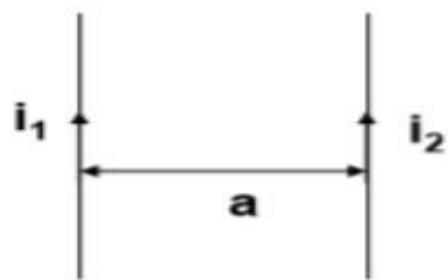
E learning :

**INDUKSI MAGNETIK (Review materi)**



# 1. Gaya Magnet

## Gaya Lorentz pada Kawat Sejajar



Medan magnet di kawat 1 akibat kawat ke-2

Gaya magnet pada kawat 2 disebabkan oleh medan  $\mathbf{B}_2$  (semua yang)

Gaya pada kawat 1 yang disebabkan oleh kawat 2

$$F_1 = \frac{\mu_0 I_1 I_2}{2\pi a} l_1$$

Gaya pada kawat 2 yang disebabkan oleh kawat 1

$$F_2 = \frac{\mu_0 I_1 I_2}{2\pi a} l_2$$

$$B_2 = \frac{\mu_0 I_2}{2\pi a}$$

$$|F_B| = I_1 l_1 |B_2|$$

$$|F_B| = \frac{I_1 l_1 \mu_0 I_2}{2\pi a} = \frac{\mu_0 I_1 I_2}{2\pi a} l_1$$

### Gaya / satuan panjang

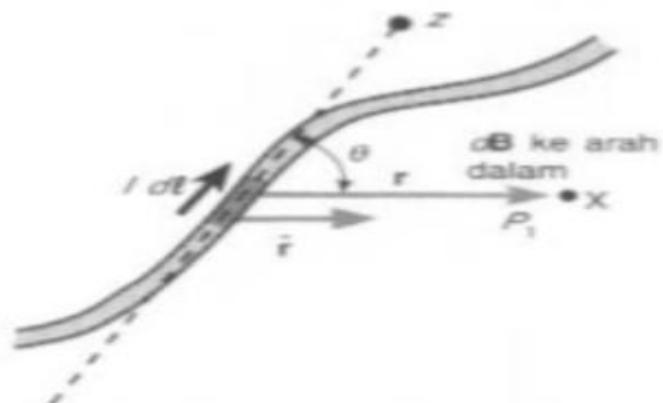
$$F = \frac{\mu_0}{2\pi} \frac{i_1 i_2}{a} l$$

Kawat yg arah arusnya **searah** akan **tarik-menarik**.  
Kawat yang arusnya **berlawanan arah** akan **tolak-menolak**



## 2. Hukum Biot-Savart

Medan magnet di sekitar elemen panjang kawat berarus adalah:



$$d\vec{B} = k_m \frac{i d\vec{l} \times \hat{r}}{r^3}$$

$$k_m = \frac{\mu_0}{4\pi} = 10^{-7} \text{ Wb / A} \cdot \text{m}$$

$\mu_0$  = permeabilitas ruang hampa

$$d\vec{B} = \frac{\mu_0 i}{4\pi} \frac{d\vec{l} \times \hat{r}}{r^3}$$

$$dB = \frac{\mu_0 i}{4\pi} \frac{dl \sin \theta}{r^2}$$

Medan magnet resultan di p:  $B = \int dB$



# Hukum Biot Savart : Kawat Lurus panjang

$$B = \int dB = \frac{\mu_o i}{4\pi} \int_{x=-\infty}^{x=\infty} \frac{dx \sin \theta}{r^2}$$

$dx$ ,  $\sin \theta$ , dan  $r$  adalah variabel

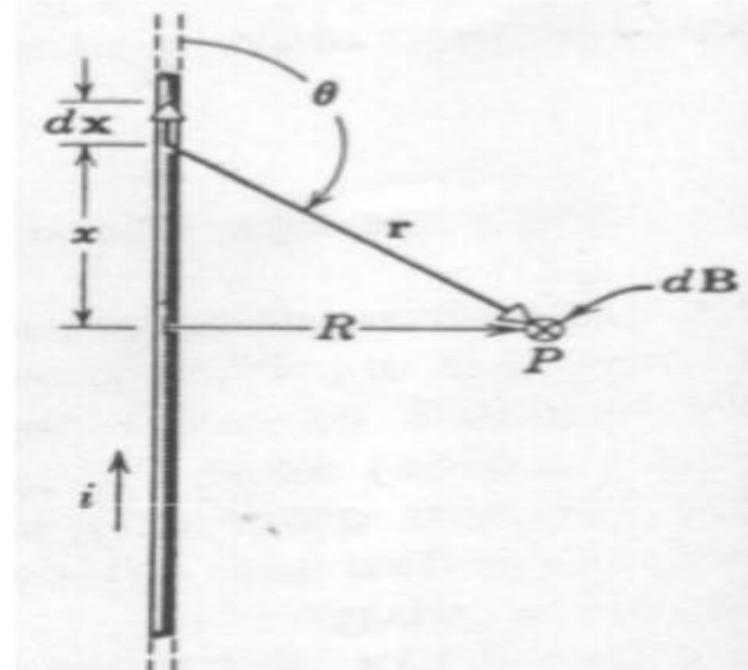
Ingat: agar integral dapat diselesaikan, maka ruas kanan harus memiliki 1 variabel

$$r = \sqrt{x^2 + R^2}$$

$$\sin \theta = \frac{R}{x} = \frac{R}{\sqrt{x^2 + R^2}}$$

$$B = \frac{\mu_o i}{4\pi} \int_{x=-\infty}^{x=\infty} \frac{R dx}{(x^2 + R^2)^{\frac{3}{2}}} \rightarrow B = \frac{\mu_o i}{4\pi} \frac{x}{(x^2 + R^2)^{\frac{1}{2}}} \int_{x=-\infty}^{x=\infty}$$

Kemanakah arah medan magnet???

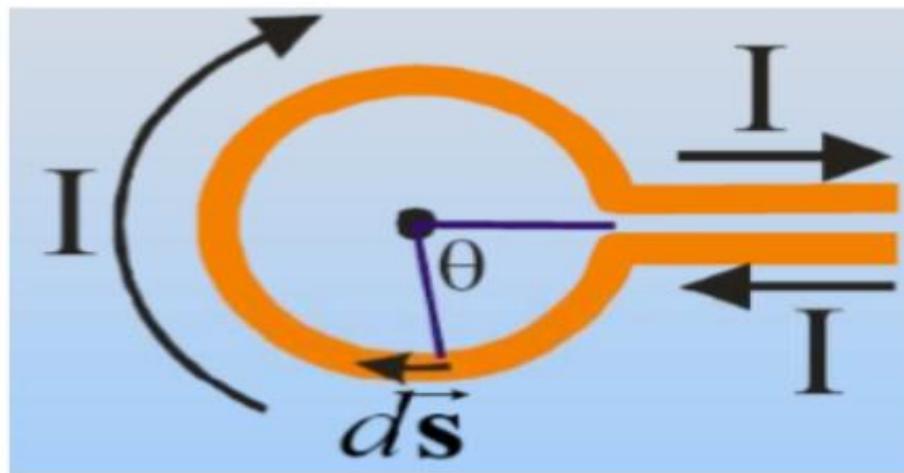


$$B = \frac{\mu_o i}{2\pi R}$$



# Hukum Biot Savart : Kawat melingkar

Tinjau sebuah koil dengan radius  $R$  dan arus  $I$



Bagaimana dengan lilitan kawat dengan radius  $R$  dengan  $N$  lilitan???

$$B = \frac{\mu_0 i N}{2R}$$

$$dB = \frac{\mu_0 I}{4\pi} \frac{d\theta}{R}$$

$$B = \int dB = \int_0^{2\pi} \frac{\mu_0 I}{4\pi} \frac{d\theta}{R}$$

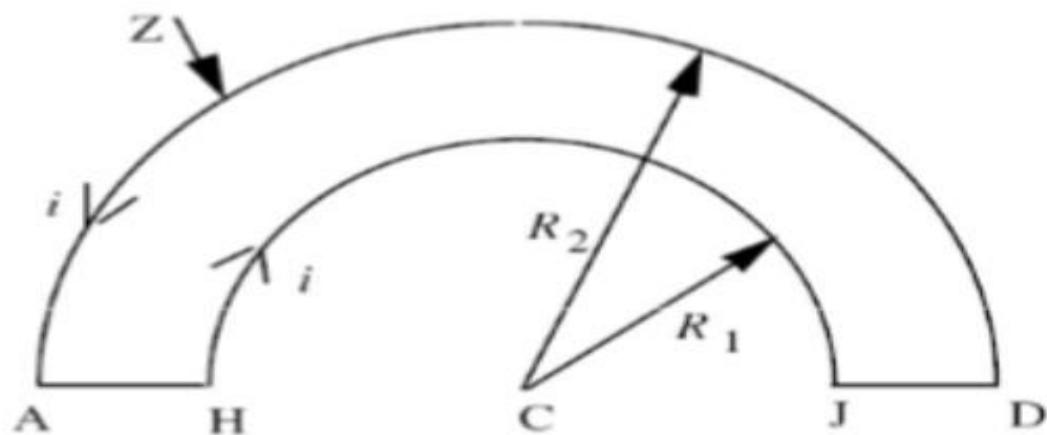
$$= \frac{\mu_0 I}{4\pi R} \int_0^{2\pi} d\theta = \frac{\mu_0 I}{4\pi R} (2\pi)$$

$$\vec{B} = \frac{\mu_0 I}{2R}$$

Masuk bidang



## Contoh Soal :



Gunakan Hukum Biot-Savart untuk Menghitung medan magnet  $B$  di  $C$ , Yakni pusat bersama dari busur-busur Setengah lingkaran  $AH$  dan  $HJ$ , yang Jari-jarinya  $R_2$  dan  $R_1$ , yang membentuk Bagian dari rangkaian  $AD/HA$  yang Mengangkut arus  $i$

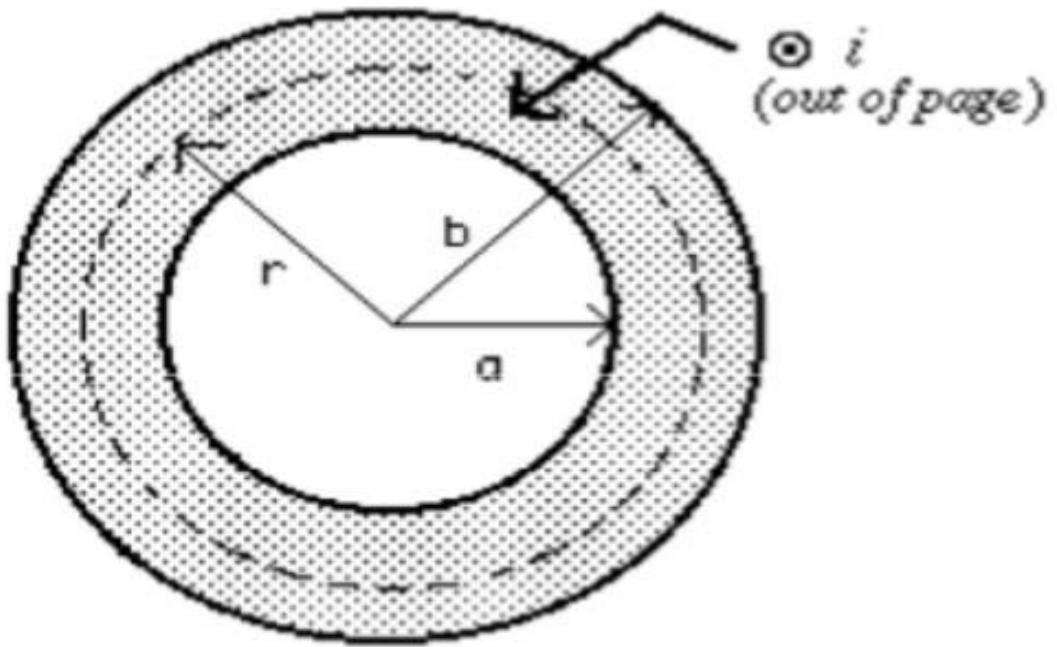
$$B = \frac{\mu_o i}{4\pi} \frac{dl \sin \theta}{r^2}$$

$$B = \frac{\mu_o i}{4\pi} \int_D^A \frac{dl}{R_2^2} - \frac{\mu_o i}{4\pi} \int_J^H \frac{dl}{R_1^2}$$

$$B = \frac{\mu_o i}{4} \left( \frac{1}{R_2} - \frac{1}{R_1} \right)$$



## Contoh soal :



Gambar di samping memperlihatkan sebuah pengantar silinder yang kosong dengan jari-jari  $a$  dan  $b$  yang mengangkut arus  $i$  yang tersebar secara uniform pada penampangnya.

- a) Perlihatkan bahwa medan magnet  $B$  untuk titik-titik di dalam badan pengantar ( $a < r < b$ )

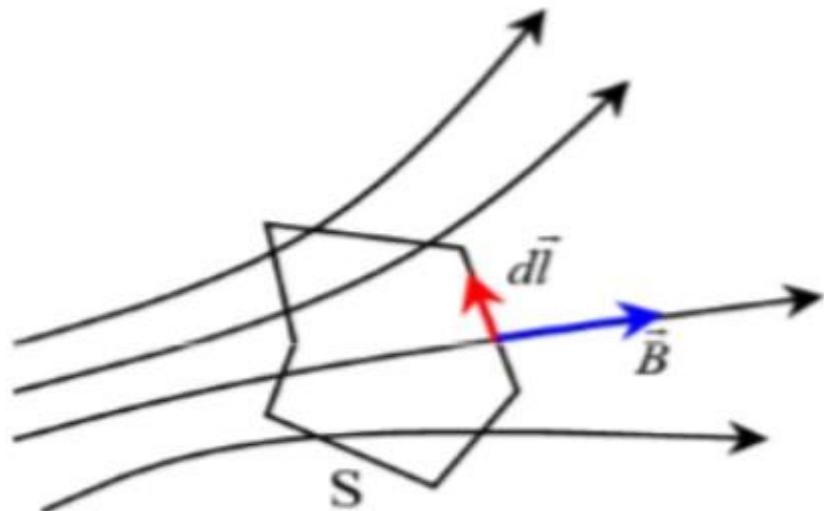
$$B = \frac{\mu_0 i}{2\pi(b^2 - a^2)} \frac{r^2 - a^2}{r}$$

- b) Buatlah gambar kasar sifat umum  $B(r)$  dari  $r = 0$  sampai  $r = \infty$



### 3. Hukum Ampere

Misalkan di suatu ruang terdapat medan magnet  $\vec{B}$ . Di dalam ruang tersebut kita buat sebuah lintasan tertutup  $S$  yang sembarang



Integral perkalian titik  $\vec{B}$  dan  $d\vec{l}$  dalam lintasan tertutup  $S$  memenuhi :

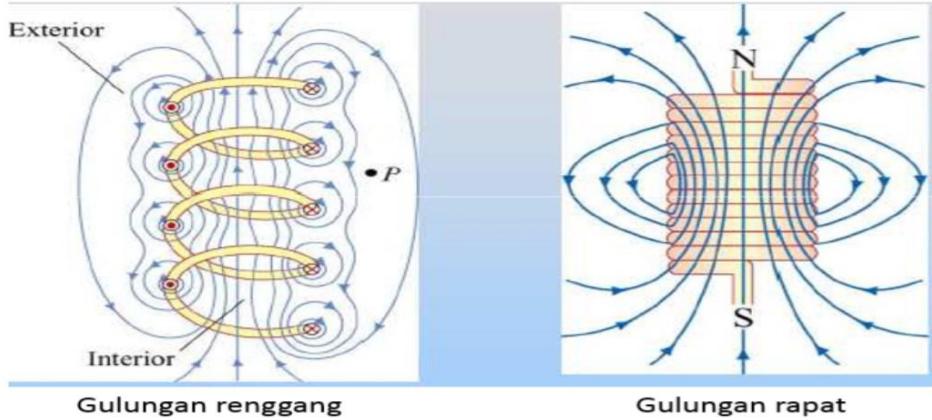
$$\oint_S \vec{B} \cdot d\vec{l} = \mu_0 \sum I \quad \text{HUKUM AMPERE}$$

$\sum I$  = Jumlah arus total yang dilingkupi lintasan  $S$

$\oint$  = Integral harus dikerjakan pada lintasan tertutup



# Aplikasi Hukum Ampere



Jumlah arus yang dilingkupi lintasan Ampere :  $\sum I = nIl$

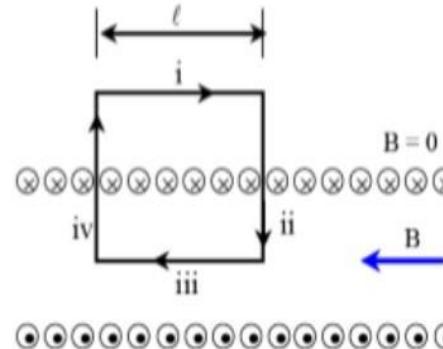
$n$  = lilitan per satuan panjang

$$\begin{aligned} \text{Maka : } \oint_S \vec{B} \cdot d\vec{l} &= \mu_0 \sum I \\ Bl &= \mu_0 (nlI) \end{aligned}$$

$$B = \mu_0 In$$

Kuat medan magnet dari selenoida

Jika selenoida dibelah



Lintasan i :  $B = \text{nol}$  (berada di luar selenoida)

$$\oint_i \vec{B} \cdot d\vec{l} = 0$$

Lintasan ii: Potongan yang ada di luar  $B = \text{nol}$   
Potongan yang ada di dalam  
 $B$  tegak lurus lintasan

$$\oint_{ii} \vec{B} \cdot d\vec{l} = \oint_{pot.luar} \vec{B} \cdot d\vec{l} + \oint_{pot.dalam} \vec{B} \cdot d\vec{l} = 0 + \oint_{pot.dalam} B dl \cos 90^\circ = 0$$

Lintasan iii :  $B$  sejajar lintasan

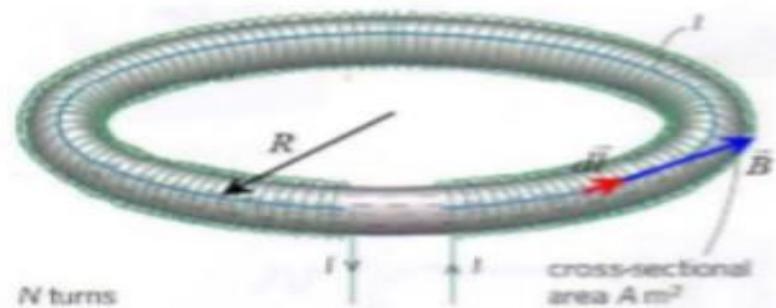
$$\oint_{iii} \vec{B} \cdot d\vec{l} = \oint_{pot.dalam} B dl \cos 0^\circ = B \oint_{pot.dalam} dl = Bl$$

Lintasan iv: Potongan yang ada di luar  $B = \text{nol}$   
Potongan yang ada di dalam  
 $B$  tegak lurus lintasan

$$\oint_{iv} \vec{B} \cdot d\vec{l} = \oint_{pot.luar} \vec{B} \cdot d\vec{l} + \oint_{pot.dalam} \vec{B} \cdot d\vec{l} = 0 + \oint_{pot.dalam} B dl \cos 90^\circ = 0$$



# Toroida



$$\begin{aligned}\vec{B} &\parallel d\vec{l} \quad \text{Sudut } \theta = \text{nol} \\ \vec{B} \cdot d\vec{l} &= B dl \cos \theta = B dl \cos 0 = B dl \\ \oint_S \vec{B} \cdot d\vec{l} &= B \oint_S dl \\ &= B \times \text{keliling lingkaran} \\ &= B \times 2\pi R\end{aligned}$$

Jumlah arus yang dilingkupi lintasan Ampere :  $\sum I = 2\pi R n I$

Maka :

$$\oint_S \vec{B} \cdot d\vec{l} = \mu_0 \sum I$$

$$B(2\pi R) = \mu_0 (2\pi R n I)$$

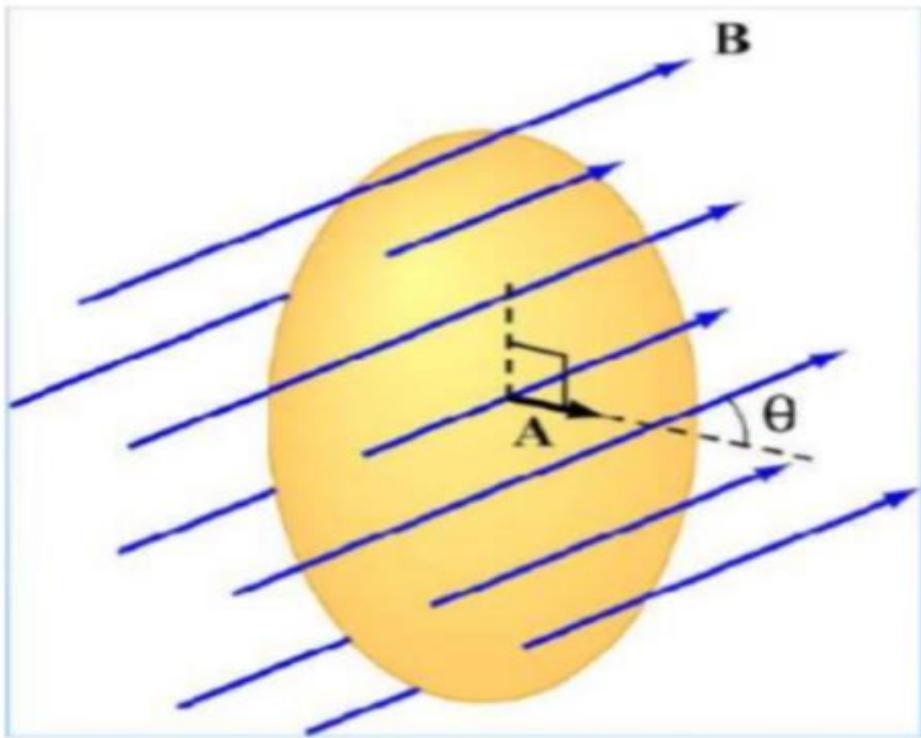
$$B = \mu_0 I n$$

Kuat medan magnet dari selenoida



# 4. Hukum Gauss Magnetik

Analog dengan Fluks Listrik (Hukum Gauss)



(1) **B Uniform**

$$\Phi_B = B_{\perp}A = BA\cos\theta = \vec{B} \cdot \vec{A}$$

(2) **B Non-Uniform**

$$\Phi_B = \int_S \vec{B} \cdot d\vec{A}$$

Animasi 8.2



## 5. Hukum Faraday

Cara untuk Menginduksi GGL

$$\mathcal{E} = -N \frac{d\Phi_B}{dt}$$

Perubahan fluks magnet  
menginduksi GGL

$$\mathcal{E} = -N \frac{d}{dt} (BA \cos \theta)$$

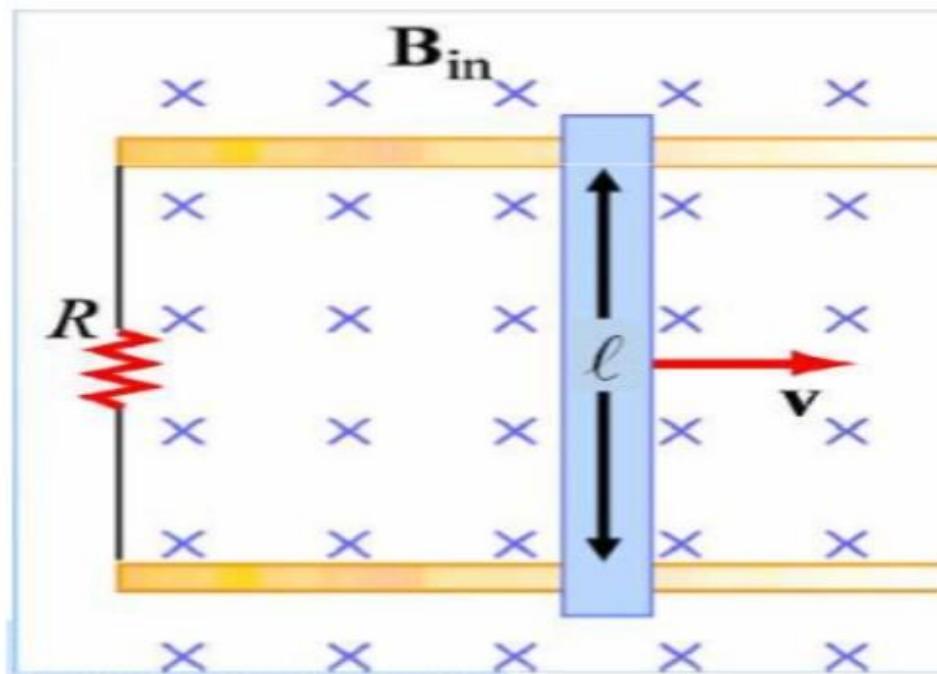
Kuantitas yang berubah terhadap waktu:

1. Besar B
2. Luas A yang dilingkupi loop
3. Sudut  $\theta$  antara B dan normal loop



## 6. Hukum Faraday : Kawat Konduktor

Batang konduktor ditarik sepanjang dua rel konduktor dalam daerah bermedan magnet uniform  $B$  dengan kecepatan konstan  $v$



1. Arah arus induksi?
2. Arah resultan gaya?
3. Besar GGL?
4. Besar arus?
5. Daya eksternal yang harus disuplai agar batang bergerak dengan kecepatan konstan  $v$ ?

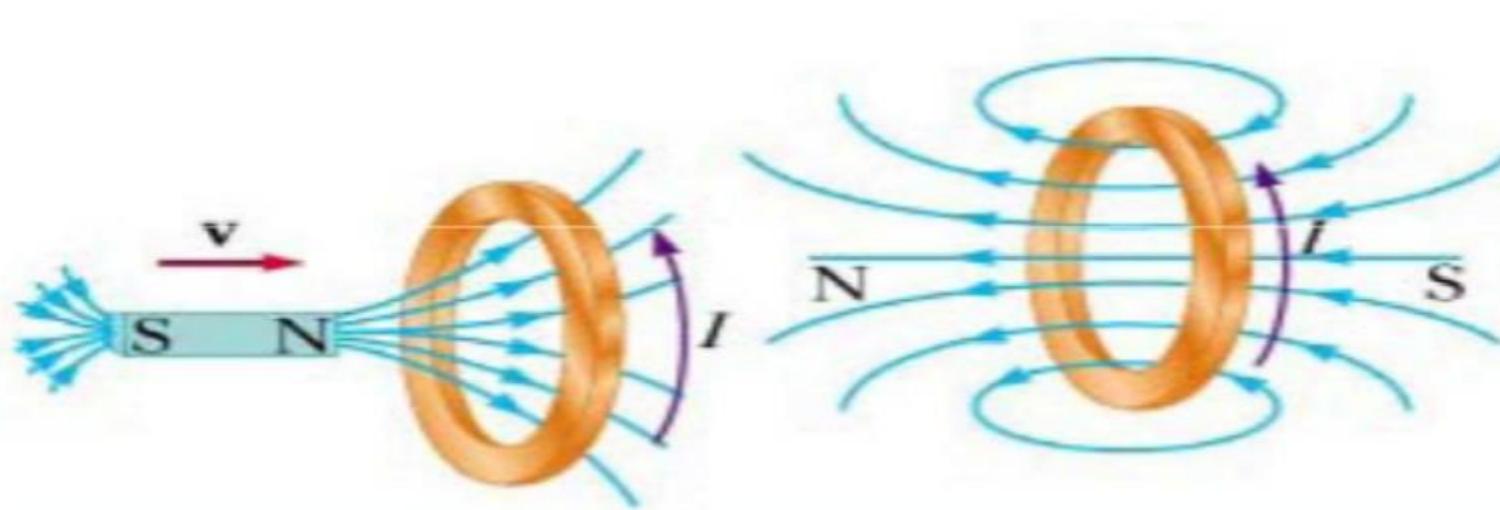
Animasi 8.6



## 7. Hukum Lenz

### Tanda Negatif? Hukum Lenz

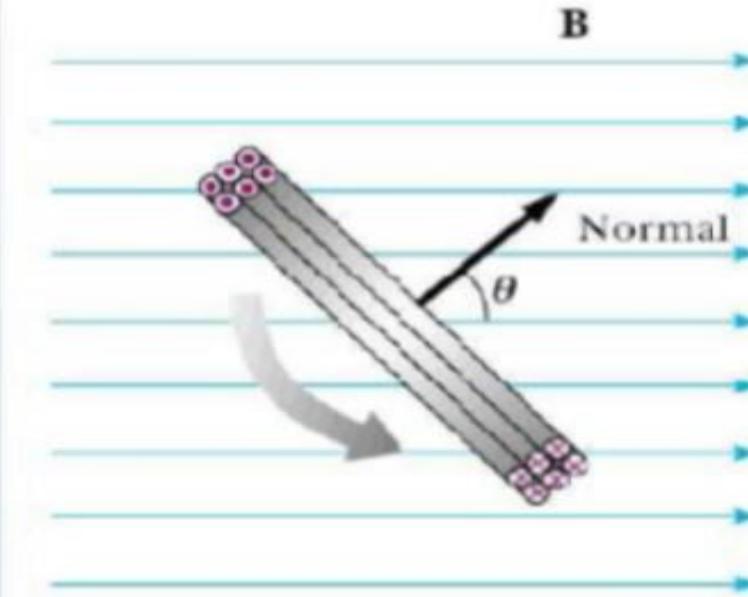
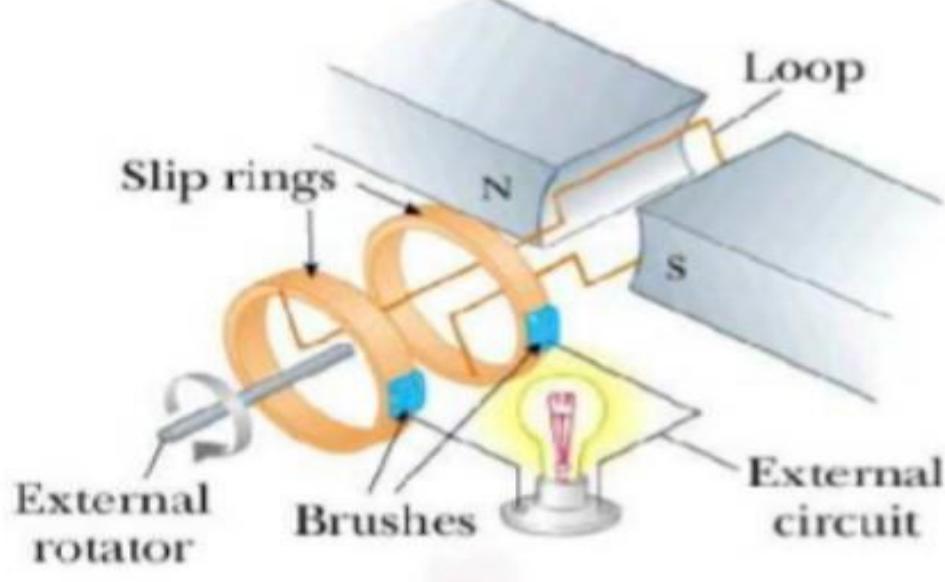
GGL Induksi yang muncul berarah melawan perubahan fluks yang menyebabkannya



**Hukum Lenz:** Arus induksi menghasilkan medan magnet yang melawan perubahan fluks magnet yang menghasilkan arus induksi tersebut



## 8. Generator



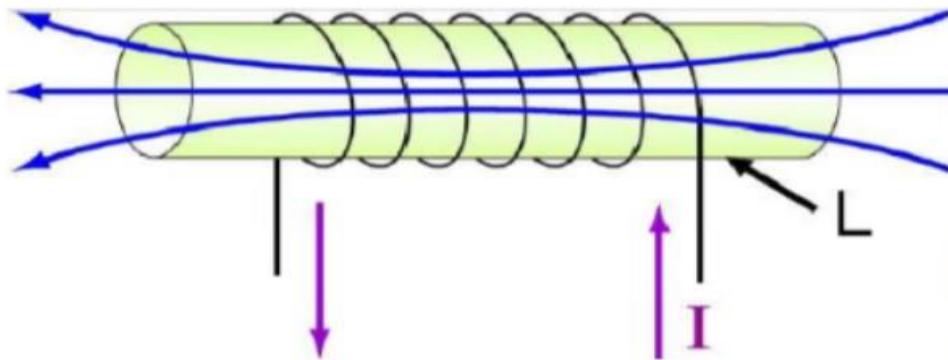
$$\Phi_B = BA \cos \theta = BA \cos \omega t$$

$$\mathcal{E} = -N \frac{d\Phi_B}{dt} = -NAB \frac{d}{dt}(\cos \omega t) = NAB\omega \sin \omega t$$

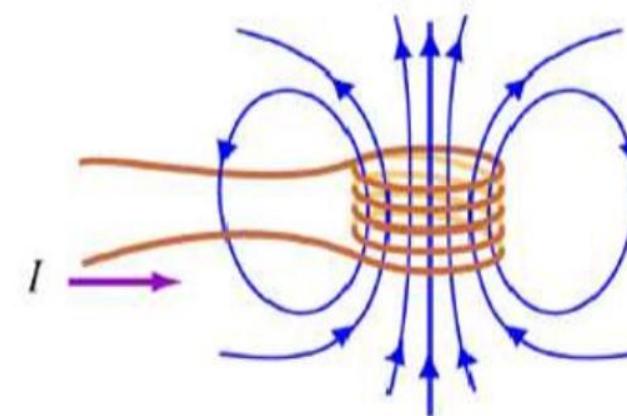


# 9. Induktansi

Sifat Induktor



$$\mathcal{E} = -L \frac{dI}{dt}$$



Induktansi Diri

Sebuah koil dialiri arus listrik.  
Arus konstan!  
Arus berubah thd waktu!

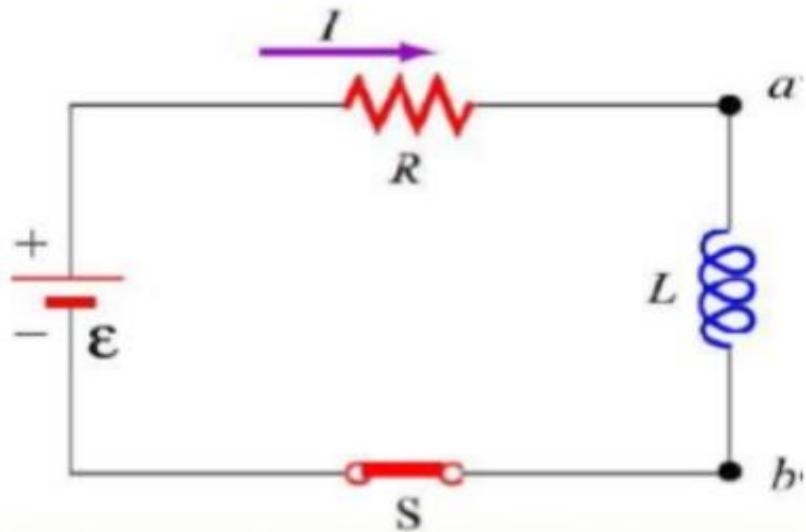
$$\mathcal{E}_L = -N \frac{d\Phi_B}{dt} = -N \frac{d}{dt} \iint \bar{B} \cdot d\bar{A}$$

$$\mathcal{E}_L = -L \frac{dI}{dt} \quad L = \frac{N\Phi_B}{I}$$

Secara fisis, Induktansi L adalah ukuran dari sebuah "resistansi" induktor untuk merubah arus; semakin besar L, semakin kecil laju perubahan arus.



## Energi Tersimpan dalam Induktor



$$\mathcal{E} = +IR + L \frac{dI}{dt}$$
$$I\mathcal{E} = I^2R + L I \frac{dI}{dt}$$

$$I\mathcal{E} = I^2R + \frac{d}{dt} \left( \frac{1}{2} L I^2 \right)$$

Batrei Penyuplai

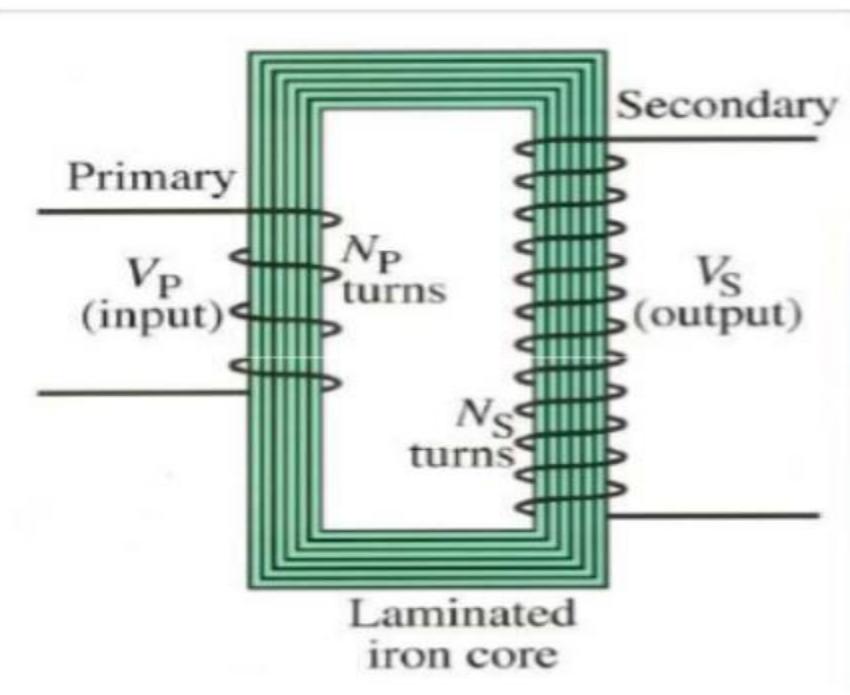
Resistor Disipasi

Induktor Penyimpan



# 8. Trafo

## Transformer



$$\mathcal{E}_p = N_p \frac{d\Phi_B}{dt}$$

$$\mathcal{E}_s = N_s \frac{d\Phi_B}{dt}$$

$$\frac{\mathcal{E}_s}{\mathcal{E}_p} = \frac{N_s}{N_p}$$

$N_s > N_p$ : step-up transformator

$N_s < N_p$ : step-down transformator



# Persamaan Maxwell

Penghasil Medan Listrik:

$$\iint_S \vec{E} \cdot d\vec{A} = \frac{Q_{in}}{\epsilon_0}$$

Hukum Gauss

$$\oint_C \vec{E} \cdot d\vec{s} = -\frac{d\Phi_B}{dt}$$

Hukum Faraday

Penghasil Medan Magnet:

$$\iint_S \vec{B} \cdot d\vec{A} = 0$$

Hukum Gauss Magnet

$$\oint_C \vec{B} \cdot d\vec{s} = \mu_0 I_{enc}$$

Hukum Ampere



Terima Kasih



# Tugas : Soal dikerjakan per individu

## EXERCISES AND PROBLEMS

### Exercises

#### Section 33.3 The Source of the Magnetic Field: Moving Charges

1. I Points 1 and 2 in FIGURE EX33.1 are the same distance from the wires as the point where  $B = 2.0 \text{ mT}$ . What are the strength and direction of  $\vec{B}$  at points 1 and 2?



FIGURE EX33.1

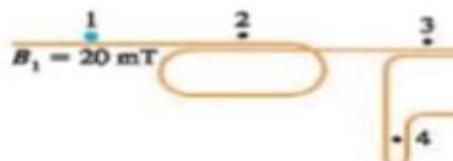


FIGURE EX33.2

2. I What is the magnetic field strength at points 2 to 4 in FIGURE EX33.2? Assume that the wires overlap closely and that points 1 to 4 are equally distant from the wires.
3. I A proton moves along the  $y$ -axis with  $v_y = -1.0 \times 10^7 \text{ m/s}$ . As it passes the origin, what are the strength and direction of the magnetic field at the  $(x, y, z)$  positions (a)  $(1 \text{ cm}, 0 \text{ cm}, 0 \text{ cm})$ , (b)  $(0 \text{ cm}, 1 \text{ cm}, 0 \text{ cm})$ , and (c)  $(0 \text{ cm}, -2 \text{ cm}, 0 \text{ cm})$ ?
4. I An electron moves along the  $z$ -axis with  $v_z = 2.0 \times 10^7 \text{ m/s}$ . As it passes the origin, what are the strength and direction of the magnetic field at the  $(x, y, z)$  positions (a)  $(1 \text{ cm}, 0 \text{ cm}, 0 \text{ cm})$ , (b)  $(0 \text{ cm}, 0 \text{ cm}, 1 \text{ cm})$ , and (c)  $(0 \text{ cm}, 1 \text{ cm}, 1 \text{ cm})$ ?
5. II What are the magnetic field strength and direction at the dot in FIGURE EX33.5?

Dikerjakan nomor 5 dan 6 saja

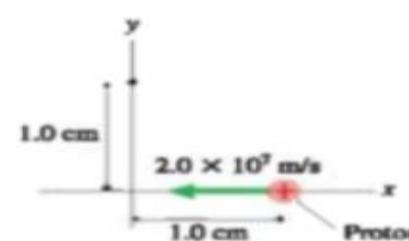


FIGURE EX33.5

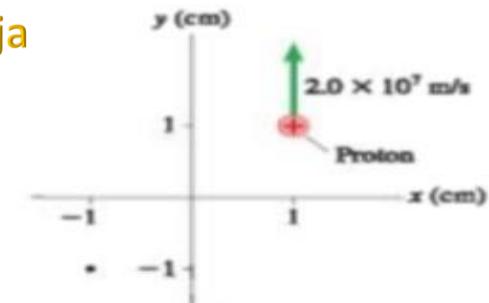


FIGURE EX33.6

6. II What are the magnetic field strength and direction at the dot in FIGURE EX33.6?
7. II A proton is passing the origin. The magnetic field at the  $(x, y, z)$  position  $(1 \text{ mm}, 0 \text{ mm}, 0 \text{ mm})$  is  $1.0 \times 10^{-13} \hat{j} \text{ T}$ . The field at  $(0 \text{ mm}, 1 \text{ mm}, 0 \text{ mm})$  is  $-1.0 \times 10^{-13} \hat{i} \text{ T}$ . What are the speed and direction of the proton?

#### Section 33.4 The Magnetic Field of a Current

8. I What currents are needed to generate the magnetic field strengths of Table 33.1 at a point  $1.0 \text{ cm}$  from a long, straight wire?
9. I At what distances from a very thin, straight wire carrying a  $10 \text{ A}$  current would the magnetic field strengths of Table 33.1 be generated?
10. II At what distance on the axis of a current loop is the magnetic field half the strength of the field at the center of the loop? Give your answer as a multiple of  $R$ .



# Tugas : Soal dikerjakan per individu

Dikerjakan nomor 12, 13, 14, 46, 47, dan 48 (semua)

12. || A wire carries current  $I$  into the junction shown in FIGURE EX33.12. What is the magnetic field at the dot?

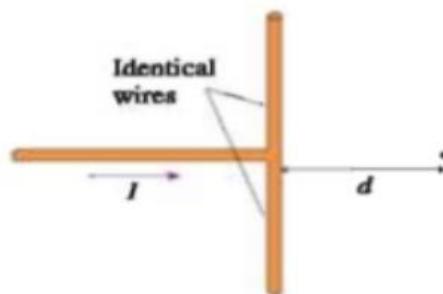


FIGURE EX33.12

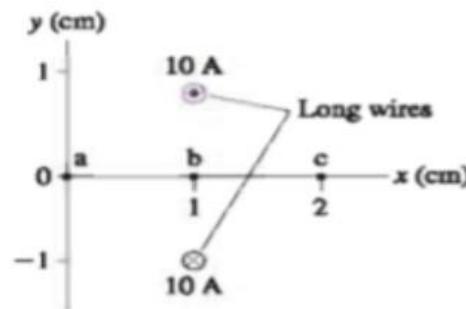


FIGURE EX33.13

13. || What is the magnetic field  $\vec{B}$  at points a to c in FIGURE EX33.13? Give your answer in component form.

14. || What are the magnetic field strength and direction at points a to c in FIGURE EX33.14?

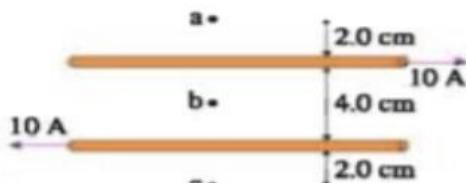


FIGURE EX33.14

46. || a. Find an expression for the magnetic field at the center (point P) of the circular arc in FIGURE P33.46.  
b. Does your result agree with the magnetic field of a current loop when  $\theta = 2\pi$ ?

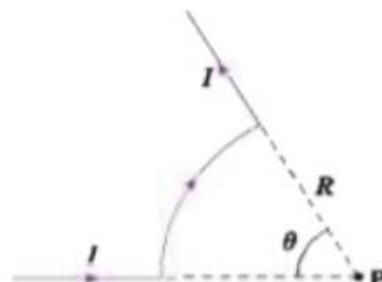


FIGURE P33.46

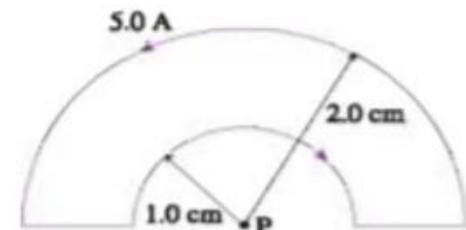


FIGURE P33.47

47. || What are the strength and direction of the magnetic field at point P in FIGURE P33.47?

48. || What is the magnetic field at the center of the loop in FIGURE P33.48?

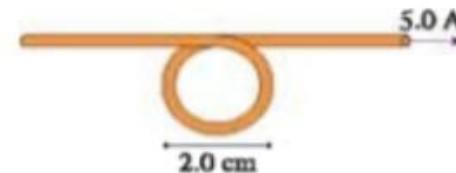


FIGURE P33.48