

Analisis Regresi

Bagian 2

Uji Keberartian Koef. Regresi

1. Susun hipotesis

$$H_0 : \beta = 0$$

$$H_1 : \beta \neq 0$$

2. Pilih tingkat signifikansi
3. Kesimpulan : tolak H_0 jika $t > t_{tabel}$

$$t = \frac{b}{s_b}$$

$$s_{y.x} = \sqrt{\frac{JK_S}{n - 2}}$$

$$s_b = \sqrt{\frac{s_{y.x}^2}{c}}, \quad c = \sum x^2 - \frac{(\sum x)^2}{n}$$

Contoh YII

1. Susun hipotesis

$$H_0 : \beta = 0$$

$$H_1 : \beta \neq 0$$

2. Pilih tingkat signifikansi α

3. Kesimpulan : tolak H_0 jika $t > t_{tabel} = t(\alpha/2, n-2)$

$$b = 0.8972$$

$$s_b = 0.166504$$

$$t = \frac{0.8972}{0.166504} = 5.388$$

Karena $t=5.388 > 2.228$ maka H_0 ditolak jadi koefisien b berarti. 2.228 diperoleh dari tabel t dengan $t(0.025, 10)$

Dengan spss..

Model Summary

Model	R	R Square	Adjusted R Square	Std. Error of the Estimate
1	.862 ^a	.744	.718	4.319

a. Predictors: (Constant), matematik

ANOVA^b

Model		Sum of Squares	df	Mean Square	F	Sig.
1	Regression	541.693	1	541.693	29.036	.000 ^a
	Residual	186.557	10	18.656		
	Total	728.250	11			

a. Predictors: (Constant), matematik

b. Dependent Variable: fisika

Coefficients^a

Model	Unstandardized Coefficients		Standardized Coefficients Beta	t	Sig.	Collinearity Statistics	
	B	Std. Error				Tolerance	VIF
1	(Constant)	29.529	9.311	.862	3.171	.010	1.000
	matematik	.897	.167				

a. Dependent Variable: fisika

Contoh 3

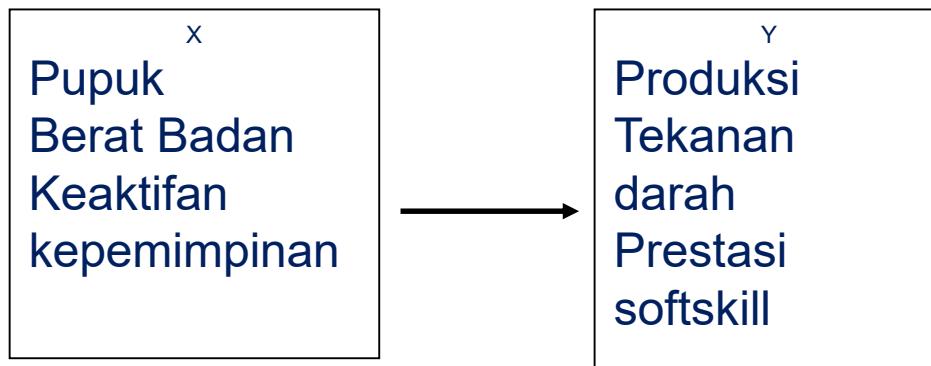
- Lakukan analisis regresi linier sederhana pada data berikut:

cerah (jam)	1.9	2.5	3.2	3.8	4.7	5.5	5.9	7.2
tiket terjual (dalam 100 ex)	22	33	30	42	38	49	42	55

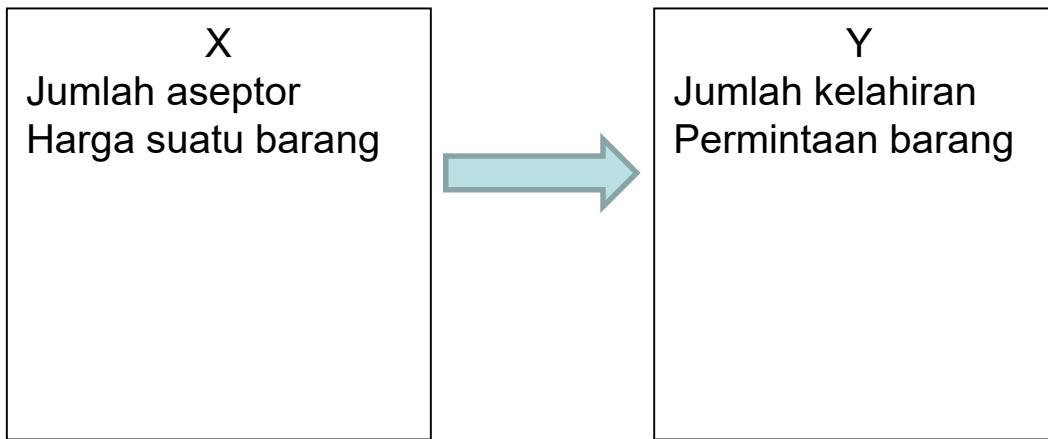
korelasi

Pada regresi linier sederhana

Ilustrasi hubungan positif

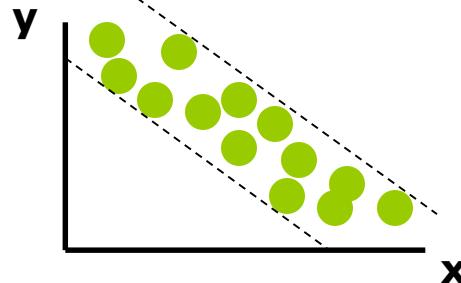
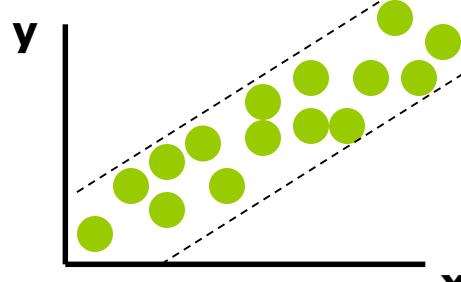


Ilustrasi hubungan negatif

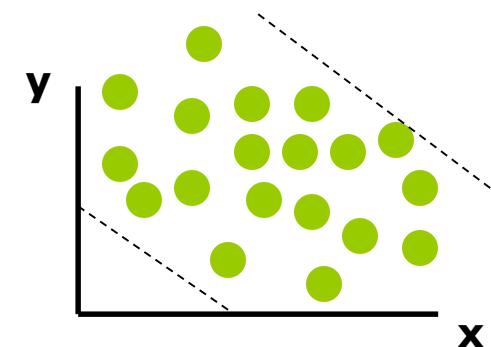
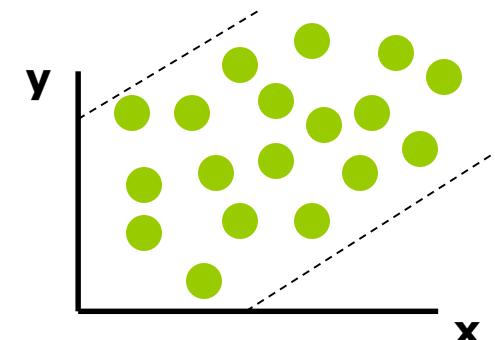


Scatter Plot Examples

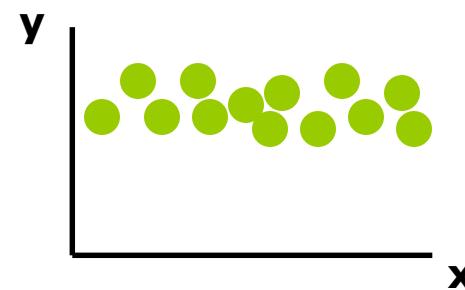
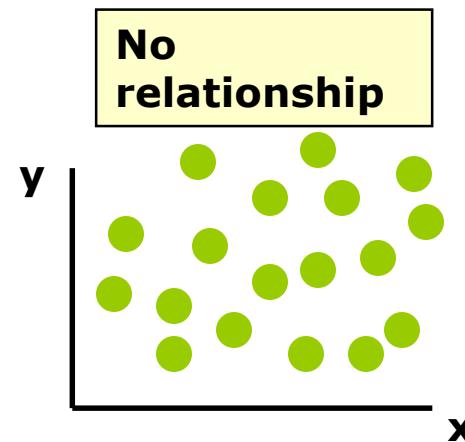
**Strong
relationships**



**Weak
relationships**



Scatter Plot Examples



Rumus r

$$r = b s_x s_y$$

b adalah slope
dari pers. regresi

standar deviasi x
dan y

$$R^2 = \frac{JK_R}{JK_T} = \frac{\text{Jumlah kuadrat yang dijelaskan oleh regresi}}{\text{Jumlah kuadrat total}}$$

Catatan: pada regresi sederhana (satu variabel bebas) koefisien determinasi dapat dinyatakan dengan dengan: $R^2 = r^2$

$$R^2 = \text{Koefisien Determinasi}$$
$$r = \text{Koefisien Korelasi Sederhana}$$

Dapatkah anda turunkan rumus r dengan JK?

Kembali ke contoh 3.

cerah (jam)	1.9	2.5	3.2	3.8	4.7	5.5	5.9	7.2
tiket terjual (dalam 100 ex)	22	33	30	42	38	49	42	55

1. Cari r dari tabel di bawah ini !
2. Tentukan jenis korelasinya !

ANOVA ^b					
Model		Sum of Squares	df	Mean Square	F
1	Regression	655.511	1	655.511	31.373
	Residual	125.364	6	20.894	
	Total	780.875	7		

a. Predictors: (Constant), X

b. Dependent Variable: Y

Coefficients^a

Model	Unstandardized Coefficients		Standardized Coefficients Beta	t	Sig.
	B	Std. Error			
1	(Constant)	15.728	4.437	3.545	.012
	X	5.336	.953		

a. Dependent Variable: Y

Kembali ke contoh 3

Jadi dapat dilihat

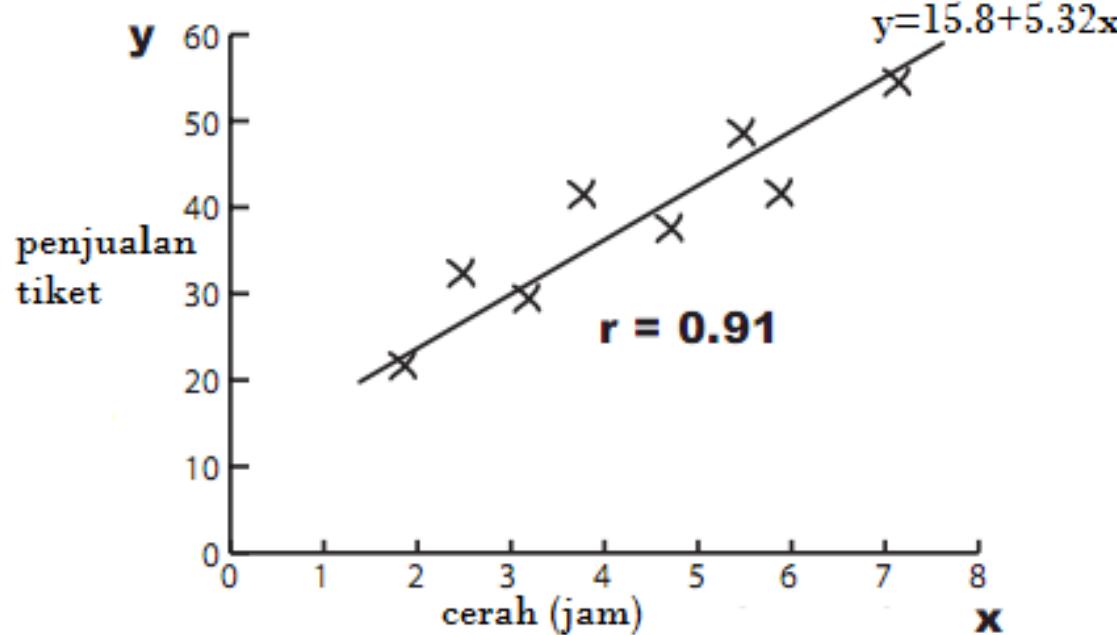
$$r = b s_x / s_y$$

$$= 5.32 \times 1.81 / 10.56$$

$$= 0.91$$

Model	R	R Square	Adjusted R Square	Std. Error of the Estimate
1	.916 ^a	.839	.813	4.57099

a. Predictors: (Constant), X



Kesalahan Baku Taksiran

(Standard Error of Estimate)

- Merupakan ukuran variabilitas antara Y dengan nilai Y prediksi

$$S_{y.x} = \sqrt{\frac{JK_S}{n - 2}}$$

ANOVA ^b					
Model		Sum of Squares	df	Mean Square	F
1	Regression	655.511	1	655.511	31.373
	Residual	125.364	6	20.894	
	Total	780.875	7		

a. Predictors: (Constant), X

b. Dependent Variable: Y

- Contoh yll:

$$JK_S = 125.364$$

$$S_{y.x} = \sqrt{\frac{125.364}{8 - 2}} = 4.57$$

Model Summary				
Model	R	R Square	Adjusted R Square	Std. Error of the Estimate
1	.916 ^a	.839	.813	4.57099

a. Predictors: (Constant), X

Kesalahan Baku Koef. Regresi

definisi

$$s_b = \sqrt{\frac{s_{y.x}^2}{c}}, \quad c = \sum x^2 - \frac{(\sum x)^2}{n}$$

Contoh 3

Contoh yll

$$\sum x^2 = 173.53, \quad (\sum x)^2 = (34.7)^2 = 1204.09$$

$$S_{y.x} = 4.57 \Rightarrow S_{y.x}^2 = 20.8849$$

$$s_b = \sqrt{\frac{s_{y.x}^2}{c}}, \quad c = \sum x^2 - \frac{(\sum x)^2}{n} = 173.53 - \frac{1204.09}{8} \\ = 23.01875$$

$$s_b = \sqrt{\frac{s_{y.x}^2}{c}} = \sqrt{\frac{20.8849}{23.01875}} = 0.952523$$

x	y	x^2
1.9	22	3.61
2.5	33	6.25
3.2	30	10.24
3.8	42	14.44
4.7	38	22.09
5.5	49	30.25
5.9	42	34.81
7.2	55	51.84
$\Sigma x = 34.7$		$\Sigma x^2 = 173.53$
$(\Sigma x)^2 = 1204.09$		

Model	Unstandardized Coefficients		Standardized Coefficients	t	Sig.
	B	Std. Error			
1	(Constant)	15.728	4.437	3.545	.012
	X	5.336	.953		

a. Dependent Variable: Y